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Impact Analysis of Electricity Supply Unreliability to Interdependent Economic Sectors by an Economic-Technical Approach

Chenghong Gu^{a*}, Xin Zhang^b, Kang Ma^a, Jie Yan^c, and Yonghua Song^d

a: Dept. of Electronic and Electrical Eng., University of Bath, Bath, BA2 7AY, U.K

b: Electricity National Control Centre, National Grid, Wokingham, U.K.

c: North China Electric Power University, Beijing, China.

d: Zhejiang University, Hangzhou, Zhejiang, China

Abstract—This paper proposes a novel framework to quantify the economic impact of electricity supply interruptions to other economic sectors considering their interdependency and increasing penetration of wind power. It is achieved by a novel integrated model that combines economic interdependency and electricity supply reliability. Leontief Input-Output model is used to determine the dependency of other economic sectors on electricity supply and electricity reliability theory is utilised to quantify electricity supply interruptions. The two models are combined to quantify two key indexes: the inoperability of different economic sectors and their losses under electricity supply unreliability. Further, an optimal model is designed to allocate available electricity to minimise the economic losses of these sectors when electricity supply is interrupted. Two UK electricity generation scenarios are used to demonstrate the concept. It is found that economic sectors have various degrees of dependency on electricity supply and their losses also differ significantly. In addition, more wind power penetration could jeopardize electricity supply adequacy and consequences to other sectors. The findings can assist policy makers to understand the importance of electricity security to other sectors and quantify potential economic losses so that new policies and regulations can be designed to mitigate the adverse consequences, such as developing the capacity market.

Keywords —Inoperability, Interdependency, Leontief input-output, Reliability, Wind power, Electricity supply.

1. Introduction

The modern society is growingly dependent on electricity supply, which is accomplished by the effort to decarbonise the energy sector to reduce greenhouse gas emissions [1]. Different economic sectors and infrastructure are now becoming closely linked, for example, natural gas and electricity systems are linked gas-fired generation and new power-to-gas techniques. The increasing interdependency brings many benefits but also challenges, where one consequence is that the failure impact in a system can propagate to others [2]. For example, the 2003 North America blackout was estimated to cause a total cost of about \$6 billion [3]. The consequence can be further worsened when electricity supply is interrupted with increasing non-dispatchable renewable, such as wind power [4].

Thus, it is essential to understand the dependency of economic sectors on electricity supply and quantify their losses in case of electricity shortage so that mitigation solutions can be adopted. Some pioneering work has studied the interdependency between electricity and other sectors from the technical

* Corresponding author. Email address: cg277@bath.ac.uk

40 aspect [5]. Paper [6] proposes an economic feasibility analysis for a standalone house operated with a
41 hybrid power plant consisting of gas generation, photovoltaic and wind generation. In [7], the authors
42 propose a new concept of energy hub which consists of various resources for energy conversion and
43 optimization. In paper [8], the authors introduce a new configuration for natural gas pressure drop stations
44 by employing a solar thermal system. The introduced concept is assessed in terms of fuel providence and
45 exergy destruction rate. Paper [9] introduces a new optimization model to analyse the interdependency
46 between different energy infrastructures, such as natural gas, coal, and electricity. It is noted that the
47 previous studies are mainly studying the physical interdependency of a limited number of energy
48 infrastructures. Due to the lack of data, they use simplified models of some sectors and networks when
49 examining the impact of failures on others. In addition, they have not quantified the economic loss of
50 one sector due to the supply failure of other sectors/infrastructure.

51 The reliability of electricity systems assesses the impact of electricity supply interruptions to other
52 sectors. Electricity system reliability mainly focuses on quantifying some key reliability indexes in
53 predefined contingency events, such as potential load loss and occurrence probabilities of the events. It
54 can be roughly divided into two categories: security which is to measure system's ability to withstand
55 stability in response to disturbances, and adequacy which is to quantify the existence of sufficient supply
56 to satisfy demand [10] [11]. In this paper, the reliability is referred to adequacy, which is also called
57 operability in economics domain. They are assumed to be interchangeable here. In quantifying the
58 economic loss of other sectors due to electricity shortage, electricity demand is normally classified into
59 various categories, such as domestic, commercial, and industrial. Each type is assigned a specific Value
60 of Lost Load (VOLL) [12] and the total economic loss is the summation of VOLL from all curtailed
61 demand [13]. This concept has served the electricity system industry for decades, but it ignores the
62 interdependency of other economic sectors, i.e. the propagating effect of electricity supply interruptions.

63 From the economic aspect, some work has investigated the impact of electricity supply interruptions
64 on other economic sectors by using Inoperability Input-Output Model (IIM). The IIM developed from
65 the original Input-Output (IO) model contributes to understanding infrastructure interdependency in
66 abnormal conditions [14]. It has been applied to many areas for risk identification and mitigation, and is
67 applicable to calculate the economic impacts of a given change to the economy. In paper [15], the authors
68 use the IIM to measure the financial and inoperability impact of the 2003 Northeast Blackout. Paper [16]
69 develops a static IO framework to analyse energy issues in the short run and discusses the potential
70 barriers to its application. Papers [17, 18] use the IIM to assess and manage inherent risks in different
71 interconnected economic systems. Paper [19] studies the marginal cost of GDP due to electricity deficits
72 but the deficit probability is predefined but not quantified. Conclusively, the disadvantage of existing
73 work in economics is that the inoperability of electricity supply is normally prefixed i.e. hypothetically
74 assumed or obtained from historical data. It is unable to reflect electricity system's stochastic features.
75 On the other hand in the electricity system domain, the impact quantification of supply unreliability is
76 fairly rudimentary, which cannot reflect the interdependency of different economic sectors. Thus, it is
77 essential to integrate the economic and technical interdependency techniques together to quantify the
78 potential impact of electricity interruptions on other economic sectors in a coherent way.

79 This paper proposes a novel integrated technical-economic framework to assess and manage the

80 unreliability of electricity supply to other economic sectors. The IIM technique is adopted to analyse the
81 economic dependency and energy system reliability is used to capture the technical dependency of other
82 economic sectors on electricity supply considering the generation of wind power. The IIM is built by
83 using national economic statistic data and the reliability of wind power is analytically modelled by a
84 Markov Model. Three key inoperability indexes are designed to measure the dependency degree of
85 different economic sectors on electricity supply. An optimal model is also introduced to manage available
86 electricity to minimise the economic losses of other sectors when electricity supply is partially interrupted.
87 The UK electricity supply scenarios with various wind penetration levels are utilized to illustrate the
88 concept. Results reveal that the proposed framework can effectively measure and manage the impact of
89 electricity supply inoperability on other sectors.

90 The key innovations of this paper are that: i) it integrates economic IIM and technical reliability
91 approaches to quantify the impact of electricity supply interruptions; ii) it designs new indexes to measure
92 the inoperability of electricity systems on other economic sectors, and iii) it studies the impact of
93 increasing wind power on the operability and economic losses of other sectors; iv) it introduces an
94 optimal management strategy to minimise the economic losses of sectors with electricity supply
95 interrupted. The study can benefit electricity system operators and policymakers to understand the
96 importance of electricity supply security and take remedy actions to ensure supply reliability to other
97 economic sectors.

98 The rest of this paper is organized as: Section 2 introduces the IO and IIM models. In section 3,
99 electricity supply reliability with wind power is presented and Section 4 defines some interdependency
100 indexes. Section 5 proposes an approach to quantify the impact of inoperable electricity supply and in
101 Section 6, an optimal management model is proposed. Section 7 employs the UK case to demonstrate
102 the proposed method. Section 8 concludes this paper.

103 2. Interdependency and The Input-output Model

104 This section briefly introduces the Leontief IO model and IIM for interdependency analysis, and the
105 application to electricity supply.

106 2.1 Leontief Input-output Model for Interdependency Analysis

107 Figure 1 illustrates the interdependency of three sectors and their external demand. By taking the
108 electricity supply as an example, one part of its output is consumed by itself, one part is exported to
109 Sectors A and B for their production, and the remaining part is to meet external demand. In turn,
110 electricity generation also needs the output from Sectors A and B to produce electricity. Thus, any deficits
111 of electricity to either Sector A or B will adversely affect electricity production. This indicates the
112 importance of considering the natural linkage/interdependency between different sectors in quantifying
113 electricity supply security.

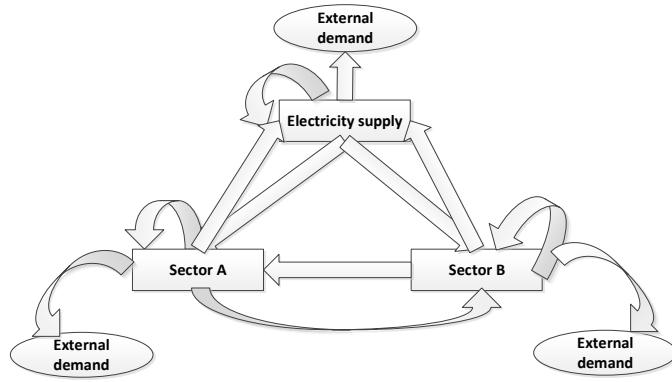


Fig.1. Input-output of a three-sector system

The Leontief IO model designed by Noble Laureate Leontief is an effective tool for examining the interactions and interdependency of different economic sectors. It provides a framework to analyse the economic impact for an equilibrium economic system with a set of interdependent subsystems or sectors. The IO model employs matrices to display the supply and demand between different sectors, called transactions table. An illustrative example is given in Table I with two sectors and one external demand column, where a row in the table displays the distribution of a producer's output and a column is the composition of inputs required by a sector in order to produce its output [20]. The total output of one section is the sum of the output to all sectors including itself and external demand.

Table I A two-sector Input-Output Table

From sector	To sector		External demand	Total output
	Sector 1	Sector 2		
Sector 1	A(1,1)	A(1,2)	C(1)	A(1,1)+A(1,2)+C(1)
Sector 2	A(2,1)	A(2,2)	C(2)	A(2,1)+A(2,2)+C(2)

Mathematically, the traditional Leontief I-O model is

$$\mathbf{X} = \mathbf{A} \cdot \mathbf{X} + \mathbf{c} \quad (1)$$

where, \mathbf{X} is the production vector, \mathbf{A} is the Leontief technical coefficient matrix, and \mathbf{c} is the final/external demand vector. All these parameters can be easily obtained by using the economic data in transactions tables [20].

Leontief inverse is defined as

$$\mathbf{B} = (1 - \mathbf{A})^{-1} \quad (2)$$

The most popular IO model is an economic formula and it can be easily transformed into an amount-based technical model to be applied for inoperability analysis [20].

2.2 Application of Input-output Model to Electricity Supply

Leontief IO model is a quantitative economic technique to represent the interdependency between different sectors of a national economy or regional economies. It has been widely used for investigating the interdependency of different economic sectors [19, 21]. It can also be applied to analysing electricity supply when it is considered to be as one sector so that its importance to other sectors can be quantified.

Take Table I as an example, where sector 1 is assumed to be the electricity supply sector. It produces

142 electricity to support its own production (with electricity amount $A(1,1)$) and that of sector 2 (with
 143 electricity amount $A(1,2)$). Meanwhile, electricity is also consumed by other external sectors/demands
 144 which do not produce products, such as domestic customers (with electricity amount $C(1)$), called
 145 external demand. Thus, if the total electricity production changes, it will affect not only its own
 146 production but also the production of sector 2 and final demand. However, the standard IO model does
 147 not provide the insight during abnormal cases and thus IIM is derived.

148 **2.3 Inoperability Input-output Model**

149 Leontief IIM proposed in [14] is widely used to evaluate the economic impact of supply perturbations
 150 in one sector on other interdependent sectors. In the model, inoperability is defined as the output
 151 difference between an as-planned scenario and the actual scenario. Electricity supply inoperability is
 152 quantified by assessing the reliability of the power system, where LOLP is defined as its inoperability
 153 index. The general form of IIM is [17]

154
$$\mathbf{q} = \mathbf{A}^* \cdot \mathbf{q} + \mathbf{c}^* \quad (3)$$

155 which can be reorganized as

156
$$\mathbf{q} = (\mathbf{I} - \mathbf{A}^*)^{-1} \cdot \mathbf{c}^* \quad (4)$$

157 where $\hat{\mathbf{c}}$ is defined as the reduced level of final demand and $\hat{\mathbf{x}}$ is the reduced level of production. Other
 158 variables in (3) and (4) are defined as follows:

159 i) \mathbf{c}^* is demand side perturbation vector expressed in terms of normalized degraded final demand

160
$$\mathbf{c}^* = [\text{diag}(\mathbf{X})](\mathbf{c} - \hat{\mathbf{c}}) \quad (5)$$

161 ii) \mathbf{A}^* is the magnitude of interdependency of sectors in an inoperable case, derived from Leontief
 162 coefficient

163
$$\mathbf{A}^* = [\text{diag}(\mathbf{X})]^{-1} \mathbf{A} [\text{diag}(\mathbf{X})]^{-1} \quad (6)$$

164 iii) \mathbf{q} is the ratio of unrealized production, defined as “as-planned” production minus degraded
 165 production divided by as-planned production

166
$$\mathbf{q} = [\text{diag}(\mathbf{X})]^{-1} (\mathbf{x} - \hat{\mathbf{x}}) \quad (7)$$

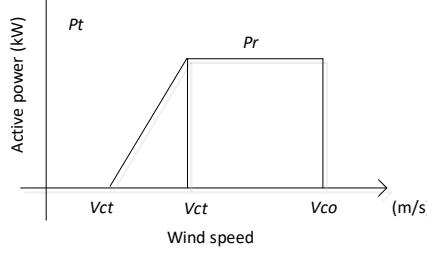
167 **3. Reliability of Electricity Supply**

168 This paper is mainly concerned with the balance between electricity supply and demand, and the
 169 impact of electricity supply unreliability on other sectors. Thus, only generation system adequacy is
 170 quantified but power system modelling is not included [22]. Normally, Monte Carlo simulation and
 171 analytical approaches are employed to assess system reliability when considering wind power. In this
 172 paper, an analytical approach is adopted here because of its simplicity.

173 **3.1 Reliability of Wind Turbine**

174 Figure 2 provides a typical wind power output curve. For simplicity, the impact of air density, swipe
 175 area of wind turbines, air pressure, etc. are not considered. A wind turbine is supposed to have the rated
 176 capacity of P_r and its actual output under each wind speed group in healthy conditions can be obtained

177 by using (8) [23]. If the wind turbine is unhealthy, the power output is assumed to be zero.



178

179 Fig.2 A typical wind turbine power curve.

180

$$P_t = \begin{cases} 0, & 0 < v < V_{ci} \\ (a + b \cdot v + c \cdot v^2) \cdot P_r, & V_{ci} < v < V_r \\ P_r, & V_r < v < V_{co} \\ 0, & v > V_{co} \end{cases} \quad (8)$$

181 where, P_t is wind turbine output, V_{ci} is wind cut-in speed, V_{co} is cut-out speed, V_r is rated output speed, P_r is rated output, and v is actual wind speed. a , b and c are coefficients.

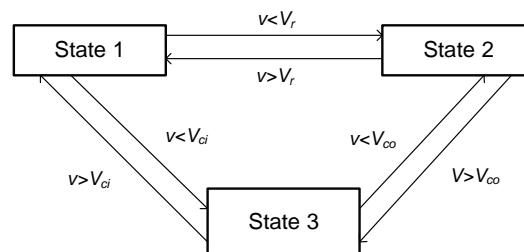
183 Because wind turbine output is between zero and its rated capacity, the active power output can be
 184 split into a finite number of steps to reduce total output states by using Markov Chain based on wind
 185 speed distributions. The transition rates and durations of all states can be obtained by analysing historic
 186 wind speed and turbine output data. For simplicity, it is assumed that a wind turbine has three states,
 187 given in Figure 3 [24]. In state 1, the wind speed is within the cut-in speed and rated output speed and
 188 thus it can produce electricity (up state); in state 2, the wind speed is within rated output speed and cut
 189 out speed and it can produce electricity (up state); in state 3, the wind speed is below cut-in speed or
 190 above cut-out speed, and thus the wind turbine is shut down (down state). The arrows between the states
 191 represent the transition of state from one to the other as long as the wind speed (indicated by v in the
 192 figure) falls into the defined group. For example, assuming the turbine initially resides in State 3 (down
 193 state), when wind speed v is bigger than cut-in speed V_{ci} but lower than rated speed V_r , it will transit to
 194 state 1. If v is smaller than cut-out speed V_{co} but higher than rated speed V_r , it will transit to State 2.

195 The classification is given in equation (9)

196

$$\begin{cases} \text{State 1 (up state):} & V_{ci} \leq v < V_r \\ \text{State 2 (up state):} & V_r \leq v < V_{co} \\ \text{State 3 (down state):} & 0 \leq V_{ci} \text{ or } v \geq V_{co} \end{cases} \quad (9)$$

197



198

199 Fig.3. State transition for a three-stage wind turbine.

200 The probability for a wind turbine to reside in each state in Figure 3 is decided by the probability of
 201 wind turbine in health status multiplied by the probability of wind speed in corresponding ranges. The

202 probability of each state thus is

$$203 \quad \begin{cases} S1: & p = (1 - FOR) \cdot p(V_{ci} \leq v < V_r) \\ S2: & p = (1 - FOR) \cdot p(V_r \leq v < V_{co}) \\ S3: & p = (1 - FOR) \cdot \{p(0 \leq v < V_{ct}) + p(v \geq V_{co})\} \end{cases} \quad (10)$$

204 where, FOR is the forced outage rate of a wind turbine and $p(\cdot)$ represents the probability of the
205 corresponding wind speed.

206 The number of wind turbine states is normally arbitrary, decided by anticipated accuracy. More
207 accurate results will need more turbine states in order to model its performance under various wind speed
208 steps. Because wind turbine and wind farm capacity is normally smaller compared to other conventional
209 generation units, thus only a few states are desirable for reducing computational burden. Once the
210 reliability modelling for a wind turbine is obtained by (10), the reliability of wind farms with multiple
211 turbines can be derived based on the single-turbine model via using Markov model. It is not covered here
212 due to space limitation and more details can be found in [25].

213 3.2 Reliability Quantification of Electricity Supply

214 Once wind farm reliability is obtained, a complete capacity outage probability table for a generation
215 system with wind power can be easily derived by a recursive algorithm through the following steps [10]:

- 216 ▪ To develop capacity model, i.e. capacity outage probability table, for individual generation unit;
- 217 ▪ To develop load model from given historic load profiles;
- 218 ▪ To combine generation capacity outage probability table with the load model to obtain the
219 probabilistic model of system capacity adequacy.

220 The final reliability indexes are the summation of those calculated in each wind speed step multiplied
221 by the occurrence probability. Mathematically, a given reliability index W can be obtained by

$$222 \quad W = \sum_{i=1}^m w_i \cdot Prob_i \quad (11)$$

223 where, w_i is the reliability index in a wind speed step i , $Prob_i$ is its probability, and m is the total number
224 of wind speed steps.

225 4. Inoperability dependency Indexes

226 Apart from inoperability, some dependency indexes are also defined in this paper to examine the
227 dependency degree of one sector on electricity supply under inoperable cases. Here, the diagonal and
228 off-diagonal elements of matrix $(I - A^*)^{-1}$ are represented by $\{a_{ii}^*\}$ and $\{a_{ij}^*\}$. Correspondingly, the
229 following three indexes are designed:

- 230 i) The diagonal entity is defined as the self-dependency inoperability index to illustrate the
231 inoperability degree of sector i due to its own output shortage

$$232 \quad \gamma_{i,i} = a_{ii}^* \quad (12)$$

- 233 ii) The off-diagonal entity is defined as the cross-dependency inoperability index to measure the
234 inoperability of sector i due to the output shortage of sector j

$$235 \quad \gamma_{i,j} = a_{ij}^*, \quad \text{where } j > i \quad (13)$$

236 iii) Index of Power Dispersion (IPD) is used to measure the impact of one sector on all other sectors,
 237 which is derived from Leontief inverse, defined as

$$238 \quad IPD_i = \frac{\sum_{j=1}^n B_{ij}}{n(\sum_{i=1}^n \sum_{j=1}^n B_{ij})} \quad (i, j = 1, 2, \dots, n) \quad (14)$$

239 where, B_{ij} is the element in Leontief inverse matrix given in equation (2).

240 The three indexes will be used in this paper to measure the importance of electricity supply to other
 241 economic sectors.

242 5. Inoperability of Electricity Supply System and Its Impact on Other Sectors

243 In this section, electricity supply reliability is integrated into the economic IIM to examine the
 244 dependency of different economic sectors on electricity supply and quantify the potential economic
 245 losses during electricity supply outage.

246 5.1 Integrating Reliability to Generation System

247 Suppose that an electricity supply system has N scenarios of generation loss and M wind speed steps,
 248 and thus in total there are $M \times N$ scenarios to be considered. In one scenario, there might be load
 249 curtailment, i.e. demand perturbation. The inoperability of electricity supply in the i^{th} wind speed state
 250 under the j^{th} generation loss case is defined as

$$251 \quad \tilde{q}_{i,j} = \begin{cases} 0 & OP_{i,j} \geq Pd_{i,j} \\ \frac{OP_{i,j} - Pd_{i,j}}{Pd_{i,j}} & OP_{i,j} < Pd_{i,j} \end{cases} \quad (15)$$

252 where, $\tilde{q}_{i,j}$ is electricity supply inoperability, $Pd_{i,j}$ is electricity system demand, and $OP_{i,j}$ is available
 253 electricity supply in the period.

254 Thus, the total electricity system inoperability is

$$255 \quad \tilde{q} = \sum_{i=1}^M \left\{ \left(\sum_{j=1}^N \tilde{q}_{i,j} \cdot Pro_j \right) \cdot Pw_i \right\} \quad (16)$$

256 where, Pro_j is generation loss probability, Pw_i is the probability of the i^{th} wind speed step, M is the total
 257 number of wind speed steps, and N is the total number of generation loss scenarios.

258 The impact of electricity supply inoperability will propagate to other sectors because of their
 259 interdependency, thus causing more perturbations in other sectors where consequence could affect in
 260 turn affect electricity production. This impact will be studied by integrating electricity system
 261 inoperability with the IIM.

262 5.2 Integration of Supply Reliability to IIM

263 Suppose that electricity supply is inoperable/unreliable and its inoperability level is specified as \tilde{q} .
 264 The final external demand perturbation is to be determined, defined as \mathbf{c}^* . For other economic sectors,
 265 their final external demand perturbations are specified beforehand and their inoperability indexes are to
 266 be determined, defined as \mathbf{q} . In a matrix format, the IIM matrix $(\mathbf{I} - \mathbf{A}^*)$ can be broken down into the
 267 following submatrices

$$268 \quad (\mathbf{I} - \mathbf{A}^*) = \begin{pmatrix} \mathbf{A}_{11}^* & \mathbf{A}_{12}^* \\ \mathbf{A}_{21}^* & \mathbf{A}_{22}^* \end{pmatrix} \quad (17)$$

269 Reorganizing (4) and submitting (17) into it produces

270
$$\begin{pmatrix} \mathbf{A}_{11}^* & \mathbf{A}_{12}^* \\ \mathbf{A}_{21}^* & \mathbf{A}_{22}^* \end{pmatrix} \cdot \begin{pmatrix} \mathbf{q} \\ \tilde{\mathbf{q}} \end{pmatrix} = \begin{pmatrix} \tilde{\mathbf{c}}^* \\ \mathbf{c}^* \end{pmatrix} \quad (18)$$

271 By resolving (18), the following solutions are obtained

272
$$\begin{cases} \mathbf{q} = \mathbf{A}_{11}^{*-1} \cdot (\tilde{\mathbf{c}}^* - \mathbf{A}_{12}^* \cdot \tilde{\mathbf{q}}) \\ \mathbf{c}^* = \mathbf{A}_{21} \cdot (\mathbf{A}_{11}^{*-1} \cdot (\tilde{\mathbf{c}}^* - \mathbf{A}_{12}^* \cdot \tilde{\mathbf{q}})) + \mathbf{A}_{22}^* \cdot \tilde{\mathbf{q}} \end{cases} \quad (19)$$

273 To summarise, the known variables are: i) inoperability level of electricity supply, i.e. unreliability, which is obtained by implementing electricity supply reliability in Section III; and ii) the final demand perturbation of other economic sectors, which are assumed to be zero if not specified. The variables to be quantified are: i) the final demand perturbation of electricity supply; and ii) the inoperability indexes of other economic sectors.

278 **5.3 Economic Loss due to Inoperability**

279 The inoperability indexes provide the impact of electricity supply interruptions to other dependent sectors. Here, an economic loss index is defined as well to capture the economic losses of other sectors 280 due to electricity supply shortage. For a specific sector, the index under each inoperable case of electricity 281 supply is quantified by multiplying the inoperability with as-planned output

283
$$Loss_k = \tilde{q}_k \cdot x_k \quad (20)$$

284 where, x_k is the planned production of sector k and \tilde{q}_k is its inoperability.

285 The total expected economic loss for sector k due to electricity supply shortage is

286
$$Loss_k = \sum_{i=1}^M \left\{ \left(\sum_{j=1}^N \tilde{q}_{i,j} \cdot Proj_j \right) \cdot Pw_i \cdot x_i \right\} \quad (21)$$

287 **6. Minimising economic loss**

288 This section proposes an optimization model to minimize the total economic loss of all other sectors 289 due to electricity supply interruptions by optimally allocating the available electricity after interruptions. 290 The control variables are allocated available electricity supply to various sectors, q_k . The objective is to 291 reduce the total economic loss for other sectors, defined in (22). At the same time, the optimisation should 292 meet three constraints: equality constraints derived from (18), upper and lower boundaries of demand 293 perturbations and sector inoperability indexes given in (23).

294
$$obj. \min cost = \sum_{i=k}^n q_k \cdot x_k \quad (22)$$

295
$$s.t. \begin{cases} \mathbf{A}_{11}^* \mathbf{q} = \tilde{\mathbf{c}}^* - \mathbf{A}_{12}^* \cdot \tilde{\mathbf{q}} \\ 0 \leq \mathbf{c}^* \leq 1 \\ 0 \leq q_k \leq 1 \end{cases} \quad (23)$$

296 where, the external demand perturbation is

297
$$\mathbf{c}^* = \mathbf{A}_{21}^* \cdot \mathbf{q} + \mathbf{A}_{22}^* \cdot \tilde{\mathbf{q}} \quad (24)$$

298 By rearranging (24) and submitting it to the first inequity in (23), the following two equations can be

299 obtained

$$\begin{cases} \mathbf{0} \leq \mathbf{A}_{21}^* \cdot \mathbf{q} + \mathbf{A}_{22}^* \cdot \tilde{\mathbf{q}} \\ \mathbf{A}_{21}^* \cdot \mathbf{q} + \mathbf{A}_{22}^* \cdot \tilde{\mathbf{q}} \leq \mathbf{1} \end{cases} \quad (25)$$

301 By reorganising (25), it produces

$$\begin{cases} -\mathbf{A}_{21}^* \cdot \mathbf{q} \leq \mathbf{A}_{22}^* \cdot \tilde{\mathbf{q}} \\ \mathbf{A}_{21}^* \cdot \mathbf{q} \leq \mathbf{1} - \mathbf{A}_{22}^* \cdot \tilde{\mathbf{q}} \end{cases} \quad (26)$$

303 The two inequality constraints in equation (26) can be integrated as one in (27), where the new
304 coefficient matrixes are formed by the coefficient matrixes of the original two inequality constraints.

$$[-\mathbf{A}_{21}^*, \mathbf{A}_{21}^*] \cdot \mathbf{q} \leq [\mathbf{A}_{22}^*, (\mathbf{1} - \mathbf{A}_{22}^*)] \cdot \tilde{\mathbf{q}} \quad (27)$$

306 This linear optimisation is resolved by many mathematical solvers, such as GAMS and CPLEX.

307 7. Case Study

308 This section uses UK electricity generation to demonstrate the proposed framework and quantify the
309 impact of electricity interruptions on other economic sectors. It also examines the optimal allocation of
310 electricity to other sectors to minimise economic loss when electricity supply shortage appears.

311 7.1 Input Data

312 Two electricity development scenarios by UK's National Grid for 2018/19, Slow Progression (SP)
313 and Low Carbon Life (LCL) under various wind penetrations are used for demonstration [26]. The LCL
314 scenario is a world of high affordability and low sustainability. High penetration of low carbon generation
315 and demand is desirable in this scenario. Government policies are mainly focused on the long-term with
316 consensus around decarbonisation, which is delivered through purchasing power and macro policy. The
317 SP scenario is a world of high affordability and low sustainability. By contrast, the penetration rate of
318 low carbon generation and demand is relatively slow compared to low carbon life scenario. Although
319 there are political wills and market interventions, slower economic recovery in this scenario delays
320 delivery against environmental targets. The UK planned electricity generation capacity in 2018-2019
321 under the two scenarios is provided in Table II. The installed capacity is 75.3GW and 79.6GW
322 respectively, and the LCL scenario has more renewable energy particularly wind power. The peak
323 demands in SP and LCL are fairly close, 54.1GW and 54.2GW respectively. The typical data from UK's
324 National Grid is used to represent electricity demand profiles [27] and the peaks are enlarged to match
325 the peaks in the two SP and LCL scenarios. The economic data from UK Office for National Statistics
326 is utilized for deriving the Input-Output model [28].

327 The availability levels of all generation technologies in the first column of Table II are from UK's
328 electricity regulator the Office of Gas and Electricity Markets (Ofgem) [29]. As seen, traditional
329 generation with relatively simple engineering complexity has much higher availability, such as pump
330 storage of 0.97, but complex generation such as nuclear has a low reliability of 0.81. Wind power plant
331 has a high reliability of 0.95.

332

333

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Table II Installed Generation Capacity in the UK (MW)

Generation	Availability	SL	LCL
Biomass	0.88	2,353	2,353
Coal	0.88	12,342	13,316
Gas-CCGT	0.94	31,408	30,346
Gas-CHP	0.94	1,699	1,544
Hydro	0.84	1,122	1,122
Nuclear	0.81	8,981	8,981
OCGT	0.94	735	735
Oil	0.82	0	0
Pump storage	0.97	2,744	2,744
Tidal	0.84	0	20
Wind	0.95	15,566	18,486
Total	N/A	75276	79647

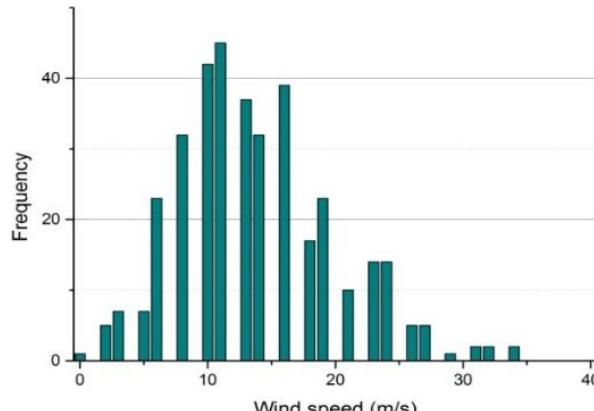


Fig. 4. Distribution of typical UK wind speed.

Table III Wind Power Output and the Probabilities

	W1	W2	W3	W4	W5	W6
Output level of wind power	100%	80%	60%	40%	20%	0%
Probability	0.32	0.19	0.24	0.09	0.08	0.08

The distribution of wind speed from a typical UK wind farm in Figure 4 is used to quantify wind power output. For simplicity, the wind power output is modelled as a generator with six output states and the following parameters are assumed: cut-in speed of 3 m/s, rated output speed of 14m/s, and cut-out speed of 25m/s. Table III gives the probability of the wind power output in relation to the total installed capacity and wind speed in Figure 4. The percentage means the output level of wind power corresponding to different wind speed. For example, the 100% output means that the wind power can produce its rated capacity output as the wind speed is above rated speed but below cut-out speed. When wind speed drops below rated speed, the output will decline as well. As seen, the wind power can provide rated power with a probability of 0.32, followed by 60% output with a probability of 0.24. For output lower than 40% of rated capacity, the probability is relatively small with a sum of 0.25.

7.2 Interdependency Analysis

By utilising the proposed method on the UK generation case, all obtained indexes are given in Table IV, including the self-interdependency and cross-dependency inoperability indexes of other sectors on electricity, and the power dispersion degree of electricity supply on other sectors.

355 As seen, electricity sector has the largest self-interdependency index of 2.21, indicating that it is the
 356 most highly dependent on its own output to produce electricity. By contrast, S7-public administration
 357 sector has the least index of 1.01, which means it is less dependent on its own output. In terms of
 358 dependency on electricity, S2-mining has the highest ratio of 0.23 followed by S4-construction sector of
 359 0.12, indicating that their production can be seriously interrupted by electricity supply shortage. The IPD
 360 reflects the dispersion level of one sector to others. When bigger than 1, it indicates the sector has a
 361 higher impact on other sectors: the higher the value is, the bigger the impact. As seen, electricity supply's
 362 IPD is 1.28, ranking the fourth after sectors S2-S4. It means that electricity supply is fairly important to
 363 other sectors. By contrast, S3-manufacturing sector has the largest IPD index of 1.68.

364

365

Table IV Indexes for all sectors

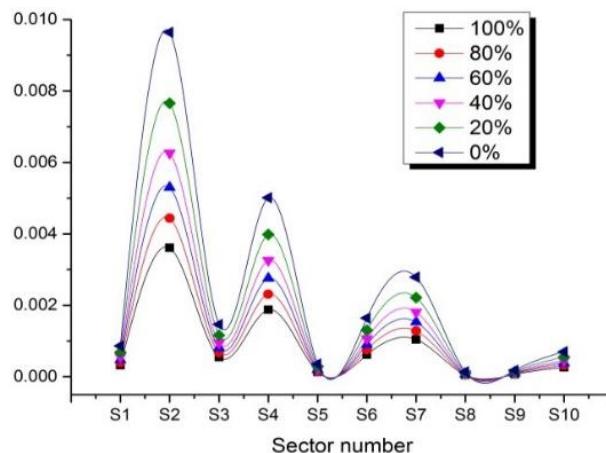
Sector	Self-dependency	On electricity	IPD
S1:Agriculture	1.39	0.02	0.92
S2:Mining	1.10	0.23	1.31
S3:Manufacturing	1.61	0.04	1.68
S4:Construction	1.97	0.12	1.61
S5:Distribution and catering	1.04	0.01	0.65
S6:Transport and communication	1.38	0.04	0.80
S7:Finance and business	1.51	0.07	0.87
S8:Public administration	1.01	0.00	0.69
S9:Education health	1.08	0.00	0.57
S10:Other	1.14	0.02	0.61
S11:Electricity	2.21	-----	1.28

366

7.3 Inoperability of Different Economic Sectors under Electricity Interruptions

367 This subsection provides the inoperability indexes of all sectors in response to electricity supply
 368 interruptions under both SP and LCL scenarios.

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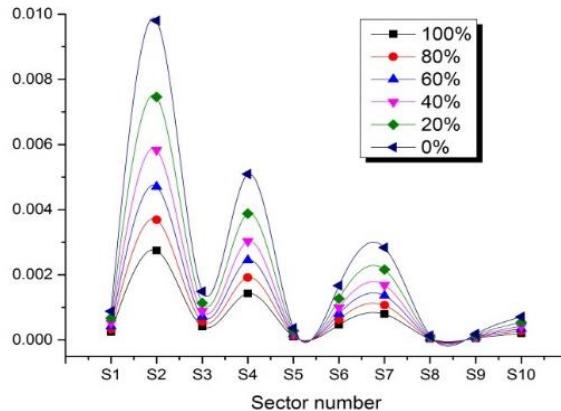
Fig.5. Inoperability under various wind speed (SP scenario).

372

373 Figures 5 and 6 are results of inoperability of all sectors under various wind speed levels from 0% to
 374 100% in Table IV. Apparently, in both scenarios, S2-mining has the highest inoperability level around
 375 0.01 with zero wind output, followed by S4-construction around 0.005. With increasing wind output,

376 inoperability indexes drop gradually. At all wind output levels, the inoperability indexes in LCL scenario
 377 are lower than those in SP scenario. It is because that although LCL scenario has slight more demand,
 378 the wind installed capacity is much higher by around 4.5GW compared to SP scenario. Thus, the shortage
 379 of electricity supply can be partially picked up by the increasing generation capacity.

380



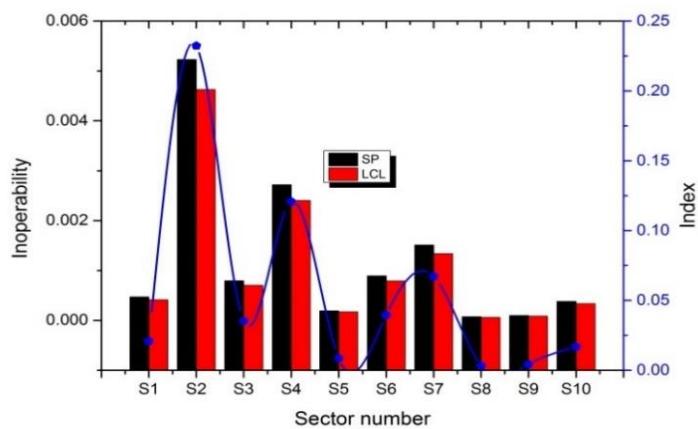
381

Fig.6. Inoperability under various wind speed (LCL scenario).

383

384 The expectations of inoperability indexes of all sectors are given in Figure 7, calculated by using the
 385 results in Figures 5 and 6. Generally, they are all lower in LCL scenario than those in SP scenario. For
 386 example, S2 has the highest inoperability indexes of 0.0052 in SP scenario and 0.0046 in LCL scenario,
 387 and S8 has the least of 0.003 and 0.001 respectively. It is mainly due to that although peak demand in
 388 LCL scenario is approximately 0.1GW higher than that in SP scenario, the installed generation capacity
 389 is also higher by 4.6GW. From another aspect, it can be seen that the inoperability indexes in the two
 390 scenarios match well with the proposed interdependency indexes on electricity supply in Table IV (the
 391 third column). For example, S2 has the biggest inoperability and its interdependency inoperability index
 392 on electricity supply is also the biggest of 0.232. By contrast, sectors S4, S7, and S6 have relatively high
 393 inoperability indexes in a descending order, which match the interdependency inoperability indexes on
 394 electricity supply as well.

395



396

Fig.7. Comparison of inoperability and interdependency indexes.

398 **7.4 Economic Loss**

399 The expected economic losses of other sectors due to electricity supply interruptions are quantified in
 400 Table V. Clearly, all sectors have higher losses in the SP scenario than in the LCL scenario. Particularly,
 401 Sector S7-finance and business suffers the largest loss of £38.77 million in SP and £34.31 million in
 402 LCL. It is because that although S7 has small inoperability indexes of 0.0015 and 0.0013 in both cases,
 403 it has the largest output of £25,642 million. Thus, small perturbations of electricity supply could cause
 404 severe disruptions to its production. It is followed by sector S4- construction with a loss of £12.16 million
 405 and £10.76 million respectively in both scenarios. Sector S8-public administration has the least economic
 406 loss across all sectors.

407

408 Table V Expected Economic Loss of Sectors (£million)

Sector	SP	LCL	Sector	SP	LCL
S1	1.08	0.96	S6	8.12	7.18
S2	5.81	5.15	S7	38.77	34.31
S3	5.60	4.96	S8	0.91	0.81
S4	12.16	10.76	S9	1.55	1.37
S5	3.21	2.84	S10	2.44	2.16

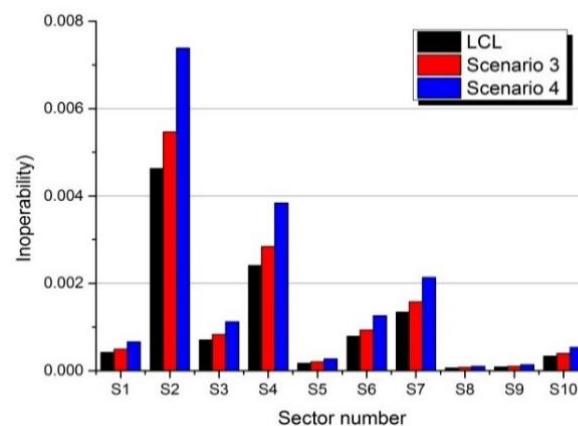
409

410 **7.5 Sensitivity Analysis of Wind Power Penetration**

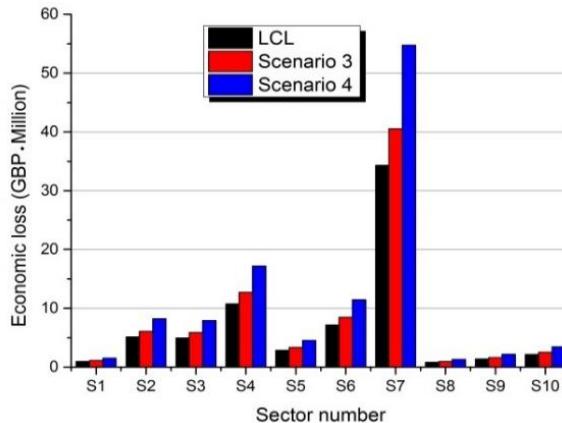
411 The impact of increasing wind power on other economic sectors is investigated by studying two extra
 412 scenarios in this subsection, scenario 3 and scenario 4. In both two new scenarios, system peak demands
 413 are assumed to be equal to that in the LCL scenario, i.e. 54.234GW. However, in scenario 3, it is assumed
 414 that 50% of coal generation is replaced with wind power, and in scenario 4 all coal generation (100%) is
 415 replaced with wind power.

416

417



418 Fig.8. Comparison of inoperability across scenarios.



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421

Fig.9. Comparison of economic loss across scenarios.

422

Figure 8 compares the inoperability indexes of all 10 sectors in LCL, 3 and 4 scenarios. Apparently, the indexes dramatically increase with more wind power penetration, particularly for those sectors severely dependent on electricity supply. For example, the inoperability of S2-mining increases from 0.0007 in LCL scenario to 0.0008 in scenario 3, and to 0.0011 in scenario 4. The values for S4-construciton and S7-finance also increase by 0.0004 from LCL scenario to scenario 3. The inoperability indexes for other sectors follow the same growing patterns.

423

The economic losses of all 10 sectors under the three scenarios are depicted in Figure 9, which also climb dramatically with increasing wind power generation. Complying with the results in Table V, sector S7 has the highest economic losses in all three scenarios, where the value is as high as £54.76 million in scenario 4. S4-construction also suffers high losses, £10.76 million, £12.71 million and £17.18 million in LCL, scenarios 3 and 4 respectively. For all sectors, S8 and S1 have the least economic losses because of their lower dependency levels on electricity supply, which are £1.29 million and £1.53 million in scenario 4.

424

The results in the two figures illustrate that the inoperability and economic losses of all economic sectors increase exponentially with growing wind power penetration. It is mainly because that wind power is relatively intermittent compared to traditional generation, and thus reliability is low. The sectors with higher dependency indexes on electricity supply have bigger inoperability indexes if electricity supply is interrupted. By contrast, economic losses are decided by both inoperability indexes and their total production, which vary over sectors.

425

7.6 Optimal Available Electricity Allocation

426

This section provides the results of optimal allocation of electricity supply to its own external demand and other sectors when the supply is interrupted. Both electricity supply inoperability and the perturbations of external demand of other sectors are assumed to be 0.1. The objective is to minimise the total economic loss of other sectors. The obtained economic losses are presented in Table VI, which are also compared with the case without optimal allocation. As seen, the total reduced cost for all sectors is £114.5 million, with sector 2 enjoying the maximum reduction of £48.2 million.

427

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429

450

Table VI Optimal Economic Loss of Sectors (£million)

Sector	Without optimisation	With optimisation	Sector	Without optimisation	With optimisation
S1	640.3	635.9	S6	612.9	604.6
S2	833.3	784.9	S7	562.5	548.5
S3	609.6	602.2	S8	252.3	251.6
S4	855.4	830.2	S9	272.5	271.6
S5	316.3	314.5	S10	362.2	358.7
			Sum	5317.3	5202.8

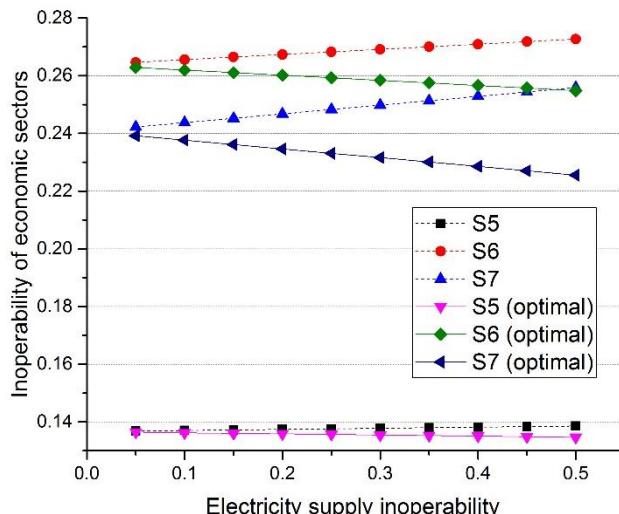
451

452 In order to obtain more insights, a sensitivity analysis of other sector's inoperability and economic
 453 losses with respect to electricity supply inoperability is conducted here in two scenarios: the old case
 454 without optimal management and with the optimal management.

455 Figure 10 provides the inoperability of three selected sectors, S5, S6, and S7. As seen, with increasing
 456 electricity supply inoperability from 0.05 to 0.5, the operability indexes of all three sectors increase,
 457 represented by the dashed lines, particularly for S6 and S7, clime very quickly. The inoperability of S5
 458 increases slightly always around 0.14 as it is less dependent on electricity supply. For the inoperability
 459 indexes in the optimal management case represented by the solid lines, they are always below those in
 460 the old case, particularly for S6 and S7 whose indexes drop with increasing electricity supply shortage.

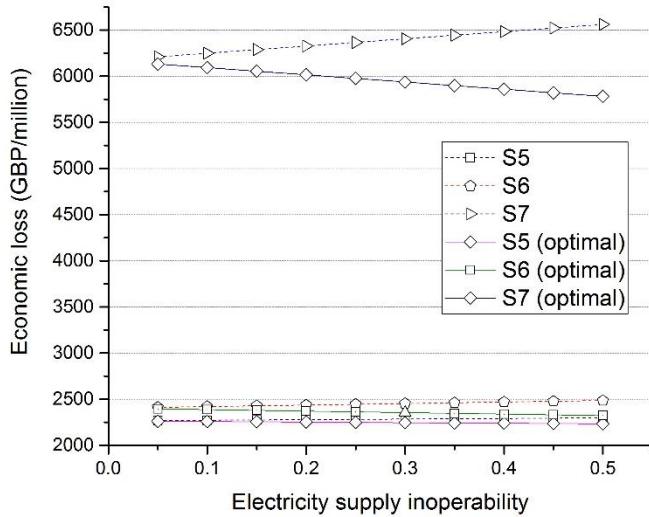
461 The economic losses of the three sectors are depicted in figure 11. Apparently, S7 has the largest
 462 economic loss in all electricity supply shortage cases with the largest, which reaches £6500 million with
 463 electricity inoperability of 0.5. This value drops to around £5700 million with the optimal management.
 464 For both S5 and S6, their economic losses are always below £2500 million in all electricity shortage case.
 465 Apparently, their losses are much lower with the optimal management compared to the case without any
 466 optimal management.

467 The results here justify that without more unreliable electricity supply, different economic sectors will
 468 suffer losses that are decided by their dependency degree on electricity and their planned output. The
 469 new optimal management can effectively reduce the losses by allocating avoidable electricity to various
 470 sectors during electricity shortage.



471

472 Fig.10. Comparison of inoperability under various electricity supply inoperability



473

474

Fig.11. Comparison of economic losses under various electricity supply inoperability

475 **8. Conclusions**

476 This paper proposes a new framework to quantify the impact of electricity supply interruptions on
 477 other sectors by introducing a novel technical-economic model. It is the first effort to integrate economic
 478 interdependency with technical electricity supply reliability for interdependency analysis. The designed
 479 indexes can effectively capture the dependency degree of economic sectors on electricity supply and
 480 their economic losses in electricity shortage. By extensive demonstration, the following key findings are
 481 observed:

482

- 483 ▪ The value of economic losses of different sectors due to electricity supply interruptions is decided
 by the scales of both inoperability indexes and their total normal production.
- 484 ▪ The growing penetration of wind power jeopardizes electricity system reliability and consequently
 affects other sectors in electricity shortage. The inoperability indexes and economic losses increase
 exponentially with increasing wind power penetration.
- 485 ▪ The proposed optimal management model can effectively reduce economic loss for other sectors
 by efficient allocating available electricity during interruptions.

486 The research can enable policymakers to understand the impact of electricity interruptions on different
 487 economic sectors and quantify their losses so that more informative policies can be designed to ensure
 488 secure electricity supply, such as the capacity market. In the future, more accurate demand profiles and
 489 detailed network models of each typical sector will be included to conduct more accurate modelling and
 490 analysis.

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