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# Volt-VAR-Pressure Optimization of Integrated Energy Systems with Hydrogen Injection

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**Abstract**—Volt-VAR optimization (VVO) has been investigated extensively in power systems. However, under the era of integrated energy systems (IES), the growing interdependencies between different energy systems complicate traditional VVO. This is further hardened by incurred gas quality problems due to the hydrogen injection in IES, produced by widely applied power-to-gas (P2G) facilitates that couple between power and gas systems. This paper develops a two-stage volt-VAR-pressure optimization (VVPO) model for PV-penetrated IES to manage the variation of system voltages while managing gas quality indices. In addition to the traditional voltage regulating devices, P2G facilities, which can mitigate fluctuating PV output via converting the surplus generation into hydrogen, are also used for voltage management. A two-stage distributionally robust optimization (DRO) based on moment information is utilized to model PV uncertainty. A semidefinite programming model is formulated and finally solved by the constraint generation algorithm. A 33-bus-20-node IES is used to verify the effectiveness of the proposed VVPO on voltage management, ensured gas quality with high economic efficiency. The proposed VVPO is applicable to injecting other green gases into gas systems while ensuring power quality and enable system operators to provide low-cost but high-quality multi-energy to customers.

**Index Terms**—Integrated energy systems, gas quality, renewable uncertainty, two-stage distributionally robust optimization, volt-VAR optimization.

## NOMENCLATURE

|                            |                                                            |
|----------------------------|------------------------------------------------------------|
| <b>A. Indices and sets</b> |                                                            |
| $t, T$                     | Index and set for time periods.                            |
| $b, B$                     | Index and set for power buses.                             |
| $n, N$                     | Index and set for nodes in gas system.                     |
| $i_e, I_e$                 | Index and set for traditional distributed generators (DG). |
| $i_g, I_g$                 | Index and set for natural gas sources.                     |
| $gt, GT$                   | Index and set for gas turbines.                            |

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|            |                                   |
|------------|-----------------------------------|
| $j, J$     | Index and set for PV systems.     |
| $l_e, L_e$ | Index and set for power lines.    |
| $l_g, L_g$ | Index and set for gas pipelines.  |
| $k_e, K_e$ | Index and set for electric loads. |
| $k_g, K_g$ | Index and set for gas loads.      |

## B. Abbreviations

|         |                                                          |
|---------|----------------------------------------------------------|
| CP      | Combustion potential.                                    |
| DG      | Distributed generator.                                   |
| DRO     | Distributionally robust optimization.                    |
| DR-VVPO | Distributionally robust- Volt-VAR-pressure optimization. |
| GCV     | Gross calorific value.                                   |
| G2P     | Gas-to-power.                                            |
| LPG     | Liquid petroleum gas.                                    |
| OLTC    | On-load tap changer.                                     |
| P2G     | Power-to-gas.                                            |
| RO      | Robust optimization.                                     |
| SG      | Specific gravity.                                        |
| SO      | Stochastic Optimization.                                 |
| VVO     | Volt-VAR optimization.                                   |
| VVPO    | Volt-VAR-pressure optimization.                          |
| WI      | Wobbe index.                                             |

## C. Parameters

|                                       |                                                                               |
|---------------------------------------|-------------------------------------------------------------------------------|
| $P_{sub,max}$                         | Maximum active power transfer of substation.                                  |
| $R_{i_e}^+, R_{i_e}^-$                | Maximum up and down reserve capacity of traditional DG $i_e$ at time $t$ .    |
| $R_{gt}^+, R_{gt}^-$                  | Maximum up and down reserve capacity of gas turbine $gt$ at time $t$ .        |
| $P_{i_e,max}, P_{i_e,min}$            | Maximum and minimum output of traditional DG $i_e$ .                          |
| $P_{i_g,max}, P_{i_g,min}$            | Maximum and minimum output of natural gas source $i_g$ .                      |
| $P_{gt,max}, P_{gt,min}$              | Maximum and minimum output of gas turbine $gt$ .                              |
| $V_{b,max}, V_{b,min}$                | Maximum and minimum voltage limit.                                            |
| $\delta^{OLTC}$                       | Size of change for each step in OLTC tap position.                            |
| $nTP_{max}^{OLTC}$                    | Maximum allowed number of switching operations of OLTC.                       |
| $\omega_{j,t}^{P,S}$                  | Forecasted active power output of renewable power generator $j$ at time $t$ . |
| $u_{pv}$                              | Associated coefficient for connecting active and reactive PV power.           |
| $PF_{pv,min}$                         | Minimum power factor of PV system $pv$ .                                      |
| $Q_{cb}^{cap}$                        | Reactive power capability for capacitor bank $cb$ .                           |
| $V_0$                                 | Reference voltage magnitude.                                                  |
| $f_{l_e}^a, f_{l_e}^r, f_{l_e,max}^r$ | Maximum active and reactive power flow of line $l_e$ .                        |
| $P_{k_e,t}, P_{k_g,t}$                | Active and reactive power load and gas load at time $t$ .                     |

|                                                           |                                                            |
|-----------------------------------------------------------|------------------------------------------------------------|
| $G_{ig,max},$                                             | Maximum and minimum output of natural gas source           |
| $G_{ig,min}$                                              | $i_g$ .                                                    |
| $Pr_{lg,max}, Pr_{lg,min}$                                | Maximum and minimum gas pressure of gas pipeline           |
|                                                           | $l_g$ .                                                    |
| $\gamma_{lg}$                                             | Coefficient for Weymouth equation.                         |
| $f_{lg,max}$                                              | Maximum gas flow of pipeline $l_g$ .                       |
| $\eta_{GT}$                                               | Conversion efficiency of gas turbine.                      |
| $\Omega_{hy}, \Omega_{LPG},$                              | Gross calorific value (GCV) for hydrogen, liquid           |
| $\Omega_{ni}, \Omega_{me},$                               | petroleum gas (LPG), nitrogen, methane and mixed           |
| $\Omega_{mix}$                                            | natural gas.                                               |
| $\rho_{hy}, \rho_{LPG}, \rho_{ni}$                        | Gas density of hydrogen, liquid petroleum gas,             |
| $\rho_{me}$                                               | nitrogen and methane.                                      |
| $E_{hy}, E_{LPG}, E_{ni}$                                 | Combustion potential index (CPI) of hydrogen, liquid       |
| $E_{me}$                                                  | petroleum gas, nitrogen and methane.                       |
| $O_i$                                                     | Oxygen index.                                              |
| $\Omega_{max}^{mix}, SG_{max}^{mix},$                     | Maximum limit for GCV, specific gravity, wobble            |
| $WI_{max}^{mix}, CP_{max}^{mix}$                          | index (WI) and Combustion Potential (CP) of mixed          |
|                                                           | gas.                                                       |
| $\Omega_{min}^{mix}, SG_{min}^{mix},$                     | Minimum limit for GCV, specific gravity (SG), WI           |
| $WI_{min}^{mix}, CP_{min}^{mix}$                          | and CP of mixed gas.                                       |
| $\Delta\varphi_{n,max}^{hy,me}, \Delta\varphi_{n,t}^{hy}$ | Maximum volume deviation for hydrogen producing            |
| $\Delta\varphi_{n,max}^{LPG}, \Delta\varphi_{n,t}^{ni}$   | methane, direct used hydrogen, LPG, nitrogen and           |
| $\Delta\varphi_{n,max}^{me}$                              | methane.                                                   |
| $\varphi_{n,max}^{mix}, \varphi_{n,min}^{mix}$            | Maximum and minimum volume for mixed gas at                |
|                                                           | node n.                                                    |
| $\Theta$                                                  | Constant in Boyle's law.                                   |
| $P_{ke,max}^{ls}, P_{kg,max}^{ls}$                        | Maximum power and gas load shedding at time $t$ .          |
| $\pi_v$                                                   | The penalty cost coefficient for penalizing the voltage    |
|                                                           | deviation.                                                 |
| $V_b^{ref}$                                               | Nominal voltage magnitude.                                 |
| $\lambda_N, \lambda_{LPG}$                                | Cost coefficients for nitrogen and liquid petroleum        |
|                                                           | gas.                                                       |
| $\lambda_{sub}^a, \lambda_{sub}^r$                        | Unit cost for active and reactive power supplied from      |
|                                                           | upper market.                                              |
| $\lambda_{ie}^a, \lambda_{ie}^b, \lambda_{ie}^c$          | Cost coefficients for generation of traditional DG $i_e$ . |
| $\lambda_{ig}$                                            | Cost coefficient for generation of natural gas source      |
|                                                           | $i_g$ .                                                    |
| $\lambda_{ie}^+, \lambda_{ie}^-$                          | Cost coefficient for up and down reserve of                |
|                                                           | traditional DG $i_e$ .                                     |
| $\lambda_{ie}^r, \lambda_j^r$                             | Regulation cost coefficient for traditional DG $i_e$ and   |
|                                                           | renewable power generator $j$ .                            |
| $\lambda_{ke}^{ls}, \lambda_{kg}^{ls}$                    | Penalty cost coefficient for power and gas load            |
|                                                           | shedding.                                                  |

In section C, the variables of both the first and second stages are represented. In the mathematical formulations, 'scheduled' and 'regulated' are represented by 's' and 're', indicating the decision variables at the first and second stages. Moreover, the 'initial' and 'terminal' for power buses and gas nodes are denoted as 'ini' and 'ter' as the superscripts.

#### D. Variables and functions

|                                       |                                                      |
|---------------------------------------|------------------------------------------------------|
| $P_{sub,t}, Q_{sub,t}$                | Active and reactive power supply from upper          |
|                                       | market.                                              |
| $r_{ie,t}^+, r_{ie,t}^-, r_{gt,t}^+,$ | Up and down reserve capacity of generators and       |
| $r_{gt,t}^-$                          | gas turbines.                                        |
| $P_{ie,t}, P_{gt,t}$                  | Output of traditional DGs and gas turbines.          |
| $V_{b,t}, V_{sub,t}$                  | Voltage of bus $b$ and substation at time $t$ .      |
| $TP_{t}^{OLTC}$                       | Tap position of OLTC at time $t$ .                   |
| $\omega_{j,t}^Q$                      | Reactive power output of PV system $j$ at time $t$ . |

|                                                                |                                                    |
|----------------------------------------------------------------|----------------------------------------------------|
| $u_{cb,t}, Q_{cb,t}$                                           | Switch status and output of capacitor bank $cb$ at |
|                                                                | time $t$ .                                         |
| $V_{b,t}^{ini}, V_{b,t}^{ter}$                                 | Voltage magnitude for initial and terminal nodes.  |
| $f_{e,t}^a, f_{e,t}^r$                                         | Active and reactive power flow at time $t$ .       |
| $G_{ig,t}$                                                     | Output of natural gas sources.                     |
| $Pr_{n,t}$                                                     | Pressure of gas node $n$ .                         |
| $f_{lg,GT,t}, P_{gt,t}$                                        | Injected gas flow and output of gas turbine.       |
| $P_{n,t}^{P2G}$                                                | Power consumed by the electrolyser.                |
| $G_{n,t}^{hy}, G_{n,t}^{hy,me},$                               | Gas output for overall P2G process, direct         |
| $G_{n,t}^{hy,d}, G_{n,t}^{me}$                                 | hydrogen injection, hydrogen during methanation    |
|                                                                | process and methanation.                           |
| $G_{n,t}^{ca}$                                                 | Required gas of carbon dioxide during methanation  |
|                                                                | process.                                           |
| $\varphi_{n,t}^{hy,me}, \varphi_{n,t}^{hy,d}$                  | Volume for hydrogen with methanation process,      |
| $\varphi_{n,t}^{LPG}, \varphi_{n,t}^{ni}, \varphi_{n,t}^{mix}$ | direct use, LPG, nitrogen, methane and mixed       |
|                                                                | natural gas.                                       |
| $\Omega_{n,t}^{mix}, SG_{n,t}^{mix},$                          | CGV, SG, WI and CP for mixed gas of node $n$ at    |
| $WI_{n,t}^{mix}, CP_{n,t}^{mix}$                               | time $t$ .                                         |
| $P_{ke,t}^{ls}, Q_{ke,t}^{ls},$                                | Power and gas load shedding at time $t$ .          |
| $P_{kg,t}^{ls}$                                                |                                                    |

## I. INTRODUCTION

IN recent years, there is an increasing need for the integration of multi-energy vectors due to decarbonization and booming coupling technologies between energy infrastructures. Integrated energy system (IES) plays a vital part through coordinating energy supply, conversion, storage and consumption between each sub-system, e.g., power, gas, heat and cooling systems. The optimal operation of IES is one significant research topic, which ensures the economy and reliability of IES. Numerous studies in the existing literature have explored the optimal operation under renewable uncertainties [1-6].

To facilitate energy conversion and tighten system couplings, the emerging power-to-gas (P2G) has been recognized as an effective technique to convert surplus renewable energy into hydrogen, transported in natural gas systems. Considering the wide deployment of gas-fired generators, bidirectional energy flows between power and natural gas systems can be realized. Paper [1] proposes an optimal stochastic optimization (SO)-based P2G operation scheme in a day-ahead gas and power market to minimize gas storage operating expenditure. A coordination framework for maximizing the profit of wind farms with P2G facilities is proposed in [2]. The bidding strategy is modelled by a SO model with a cooperative game framework. Paper [7] designs a decentralized P2G operation scheme considering linearized transient-state gas flow. In general, inherent renewable uncertainty in IES impacts i) P2G conversion, ii) gas quality management, iii) voltage regulation, and iv) whole system operation.

Hydrogen can be injected into gas systems after being produced from P2G facilities. Consequently, the original gas composition would inevitably be changed due to hydrogen injection. The impact will further propagate to the gas system, affect the gas quality of end customers, and cause security problems [8]. Paper [9] proposes a simulation for the unsteady operation of natural gas systems with hydrogen injection. The risk assessment involves the change of gas composition, flow

rate and pressure profile, compared to the case without hydrogen injection. An assessment of the safety and working performance of gas appliances with the admixture of hydrogen is studied in [10]. In previous studies, the most common gas quality index to measure gas interchangeability is Wobbe index (WI). The influence of fuel variability on flame surface, flame normal and WI are investigated for hydrogen-enriched combustion in [11]. WI is used to measure the efficiency of combustion of syngas mixtures. Paper [12] utilizes WI as a pivotal standard to investigate the impact of WI on interoperability between different gas components. Gas interchangeability is studied in [10] based on WI, indicating that WI is highly associated with flashback issues and thus is essential to consider. To maximize the hydrogen production, the required level of WI and combustion potential (CP) for secure hydrogen operation is proposed in [13].

Although the interaction between each sub-system facilitates system economic performance and security, it also raises challenges to VVO as the system topology is changed and the bidirectional energy flow complicates the operation. Volt-Var-Optimization (VVO) is an essential requirement for distribution power systems to mitigate voltage deviations, reduce power losses and achieve reliable and economic system operation [14, 15]. VVO determines the optimal set of operation actions via voltage regulating devices, e.g., voltage regulators, on-load tap changers (OLTC), capacitor banks and renewable inverters [16]. Under the extensive renewable penetrated era, the rapidly growing penetration of renewable technologies will inevitably cause voltage fluctuations and affect the operations of voltage regulating devices. VVO models with optimal coordination of voltage regulating devices have been investigated widely in the existing literature and most papers consider renewable uncertainty for mitigating the resulted adverse impacts. Paper [17] deploys robust optimization (RO) to handle renewable uncertainty to ensure the economic coordination of all the devices, thus minimizing voltage deviations. The reformulated second-order cone programming model is solved by an improved column-and-constraint generation algorithm. Chance-constrained programming is utilized to model uncertain distributed generation and load demand simultaneously [18]. Paper [19] designs a game-theoretic VVO considering uncertain renewable generation, the mobility of electric vehicles and the demand response of microgrid customers. The uncertainties of renewable generation and mobility of electric vehicles are mitigated via setting short time slots.

The interdependencies in IES is enormous and the operation on a certain sub-system will propagate to other sub-systems. For instance, in an integrated electricity and gas system, the voltage regulation measures taken on the power system will influence the power and gas exchange, which eventually impacts the security and economic performance of the entire system. Moreover, gas systems can absorb surplus power generation via P2G facilities. Therefore, the study of VVO in IES is essential. The gas quality problem not only affects end customers but pressure scheduling and gas flow management of the gas system. The adjustment measures to maintain gas quality in the gas system then inevitably influences the VVO of the entire IES. An IES operator needs to ensure the secure, reliable and economic operation of electricity and gas systems. Therefore, gas quality

and pressure management are regarded as equally significant as the VVO problem in the electricity system.

To capture renewable uncertainty, this paper applies the innovative two-stage distributionally robust optimization (DRO) to hedge against uncertain renewable fluctuations. As an alternative to traditional RO and SO, DRO provides more flexibility based on partial distribution information with a predetermined ambiguity set, which does not require the specific distribution assumption while mitigating the conservatism of RO [20-22]. Therefore, the impacts on VVO and P2G operation due to renewable uncertainties can be mitigated by using DRO. Here, PV uncertainty is handled by the moment-based ambiguity set in a two-stage framework, where the first stage provides the initial scheduling scheme based on predicted PV output and the second stage recourse decisions are determined when PV uncertainty is realized. Dual formulations are made for the original problem with the resulted semidefinite programming (SDP) reformulation with tractability, which can be solved efficiently by most current commercial solvers.

In summary, three main research problems and gaps in existing research are required to be resolved: i) P2G facilities can help absorb surplus renewable output with high fluctuation and mitigate voltage deviations, but has not been used yet; ii) gas quality issues due to hydrogen injection have not been considered in IES operation; and iii) VVO problem has been extensively studied in power systems whilst has never been investigated in IES with system interdependencies;

In this paper, a novel two-stage DRO for regulating voltage deviation, managing gas quality and guaranteeing optimal system operation is proposed in an IES. To mitigate voltage fluctuations, the optimal coordination of OLTCs, capacitor banks, PV systems and P2G facilities are used as voltage regulating measures. Gas quality is also ensured based on the proposed innovative gas quality and pressure management strategy, i.e., purchasing and mixing additional liquid petroleum gas (LPG) and nitrogen to maintain satisfactory gas quality indices. The proposed volt-VAR-pressure optimization is referred to as VVPO for simplicity. Comprehensive case studies are carried out to validate the effectiveness of the distributionally robust-VVPO (DR-VVPO) model.

The major contributions are as follows:

- 1) This paper is the first attempt to study the fundamental VVO problem in IES, considering energy interdependencies and couplings.
- 2) P2G facilities are considered for alleviating voltage deviations and PV fluctuation in addition to the traditional voltage regulating devices.
- 3) A gas quality management strategy is developed in the IES operation model, where gas pressure and quality indices are constrained within an acceptable range.
- 4) A two-stage DRO approach is used to handle PV uncertainties, which avoids assuming the explicit uncertainty distributions compared with SO-based VVO and mitigates the conservatism compared with RO-based VVO.

The rest of this paper is structured as follows. Section II describes gas quality indices and P2G modelling. Section III proposes the IES model. The ambiguity set of DRO is illustrated in section IV. Section V concludes the paper.

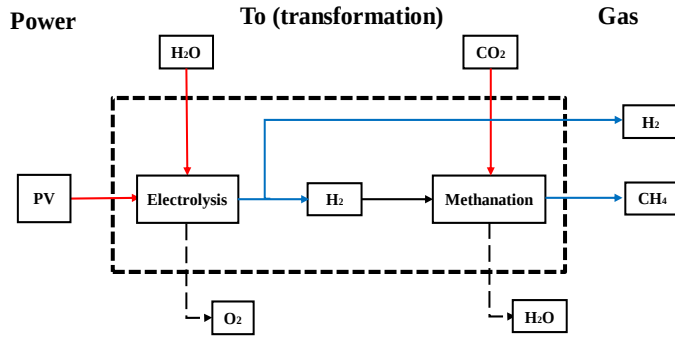


Fig. 1. The P2G process.

## II. THE PROPOSED VVPO FRAMEWORK

### A. Volt-VAR Optimization Framework

As one of the fundamental functions in distribution systems, VVO maintains voltage profile within acceptable ranges, reduces power losses and ensures system economic operation. In this paper, VVO is achieved by determining the optimal set of controlling voltage regulating devices, e.g., OLTC, capacitor banks and PV regulation. The mathematical formulation of the proposed VVO framework is given as below. The voltage magnitude at each bus is constrained in (1). Equation (2) shows the expression of the voltage at the substation. Considering the wearing process of the transformer, the total number of OLTC operations is restricted in (3). Constraint (4) limits the PV reactive power support with the regulation coefficient defined in (5). The reactive power output of capacitor banks is shown in (6). And the linearized DistFlow equation for power flow in distribution systems is presented in (7). This equation is obtained based on the assumption that i) losses are negligible, ii) the voltage at each bus is close to 1.0 p.u. and iii) the voltage at the reference bus is 1.0 p.u. [23-25].

$$V_{b,min} \leq V_{b,t} \leq V_{b,max} \quad (1)$$

$$V_{sub,t} = V_{sub}^{ref} + \delta^{OLTC} TP_t^{s,OLTC} \quad (2)$$

$$\sum_{t \in T} |TP_t^{OLTC} - TP_{t-1}^{OLTC}| \leq n TP_{max}^{OLTC} \quad (3)$$

$$-u_{PV} \omega_{j,t}^P \leq \omega_{j,t}^Q \leq u_{PV} \omega_{j,t}^P \quad (4)$$

$$u_{PV} = \sqrt{\frac{1 - PF_{PV,min}^2}{PF_{PV,min}^2}} \quad (5)$$

$$Q_{cb,t} = u_{cb,t} Q_{cb}^{cap} \quad (6)$$

$$V_{b,t}^{ini} - V_{b,t}^{ter} = (f_{l_e,t}^a r_{l_e} + f_{l_e,t}^r x_{l_e}) / V_0 \quad (7)$$

### B. Gas Quality Management

This paper ensures gas quality via four gas quality indices, i.e., WI, CP, specific gravity (SG) and gross calorific value (GCV). This section describes four indices and P2G modelling. The gas quality problems caused by the large variety are inevitable since i) many countries rely highly on gas imports and ii) different gas generation companies share the same gas transportation network. As the two most significant features for assessing the gas quality, gas adaptability and gas

interchangeability are mostly employed for quality measurement. The gas adaptability is used to describe if the gas-fired appliances work under normal conditions with the variation of gas compositions. The gas interchangeability is used to describe the operational performance of gas facilities with regards to safety, emissions and efficiency. Overall, the variation of gas composition is permitted but it needs to be controlled within an acceptable range.

SG is described in (8) by the ratio of gas density over the air density [8, 26]. This paper applies SG to limit hydrocarbon content. The density of air, hydrogen and gas is denoted as  $\rho_{air}$ ,  $\rho_{hy}$  and  $\rho_g$ , respectively. The hydrogen volume is represented by  $\varphi_{hy}$ . If the hydrocarbon content is at a relatively high amount, a series of combustion issues will be caused, e.g., more carbon monoxide emissions and spontaneous ignition events, etc.

Calorific value is used to define the amount of released heat during the gas combustion. In addition to that, GCV describes the amount of released heat when it is fully condensed and recovered, i.e., the gas temperature before and after the combustion is the same. GCV is required to restricted within a predetermined range. The expression of GCV of the mixed gas is given in (9) [27, 28], where the GCV value of gas and hydrogen are denoted as  $\Omega_g$  and  $\Omega_{hy}$ .

The measurement of gas combustion stability can be realized based on CP which characterizes the combustion features including flame issues and combustion flame and so forth. When the gases are interchangeable, the CP of each gas component should be close to each other. In (3), CP is defined, where the volume of hydrocarbon, carbon dioxide and methane are represented by  $\varphi_{cm}$ ,  $\varphi_{hc}$  and  $\varphi_{me}$ , respectively [8, 13].

WI is a measure of interchangeability of gases that compares the combustion output of different gas components. Gas components are appropriate for a mixture when the WI of gases are close to identical. However, WI of each gas component is allowed to vary within 5-10%. If the variation is beyond the allowed range, the effects will be noticeable, e.g., high greenhouse gas emission and stability issues of gas equipment. Furthermore, the immediate WI variation will lead to emergency shutdowns of gas turbines, which has an adverse impact on the longevity of gas turbines. Equation (4) presents the expression of WI [29, 30].

P2G facilities enable to convert the abundant renewable generation to hydrogen. The process of the conversion via P2G is depicted in Fig. 1. In the first step, the electrolyser is applied to split water into hydrogen and oxygen powered by excessive renewable generation. Then methane is obtained with the addition of carbon dioxide in the methanation process. Meanwhile, the produced hydrogen can be directly injected into the gas system. The P2G output is given in (5). Equations (6)-(8) present methane production and the required amount of carbon dioxide according to Sabatier factors [31].

$$SG = \frac{\rho_g + (\rho_{hy} - \rho_g) \varphi_{hy}}{\rho_{air}} \quad (8)$$

$$\Omega = \Omega_g + (\Omega_{hy} - \Omega_g) \varphi_{hy} \quad (9)$$

$$CP = O_i \frac{\varphi_{hy} + 0.6(\varphi_{cm} + \varphi_{hc}) + 0.3\varphi_{me}}{\sqrt{SG}} \quad (10)$$

$$WI = \frac{\Omega}{\sqrt{SG}} \quad (11)$$

$$G_{n,t}^{hy} = \eta_e \frac{P_{n,t}^{P2G}}{\Omega_{hy}} \quad (12)$$

$$G_{n,t}^{hy,me} + G_{n,t}^{hy,d} = G_{n,t}^{hy} \quad (13)$$

$$G_{n,t}^{ca} = \eta_{hy-ca} G_{n,t}^{hy,me} \quad (14)$$

$$G_{n,t}^{me} = \eta_{hy-me} G_{n,t}^{hy,me} \quad (15)$$

### III. SYSTEM MODELLING

In this paper, the two-stage DR-VVPO contains i) day-ahead voltage management involving maintaining voltage magnitude, determining optimal dispatch scheme of generators and ensuring satisfied gas quality and ii) real-time active adjustment based on the day-ahead optimization under the fluctuation of PV output. TABLE I summarizes all the decision variables with objectives and uncertainty treatment defined.

#### A. Day-Ahead Constraints of DR-VVPO

In the first stage, the day-ahead optimization is based on the forecasted renewable output before its uncertainty realised. Equations (1)-(7) and (16)-(39) are constraints of day-ahead DR-VVPO. The power purchase from the substation in the day-ahead upper-level energy market is limited in (16). For gas turbines and traditional DGs, the up and down reserve capacity is limited in (17) and (18). Constraints (19) and (20) regulates the output of traditional DGs and gas turbines. Constraint (21) limits the power flow magnitude. The balance constraints of active and reactive power are in (22) and (23).

In regards to the gas system, the constraints are shown in (5)-(8) and (24)-(39). The gas source output and pressure are limited in (24)-(26). Constraint (26) ensures the gas pressure at the initial gas nodes is higher than terminal nodes in the radial gas system. The gas flow is restricted between and upper and lower limits in (28). The output of the gas turbine is shown in (29). The theoretical constraints (1)-(4) are given as (30)-(33) under the real application. To guarantee the proposed gas quality indices are within the associated standard, constraint (34) is proposed. The deviation of the volume of each gas component between time slot  $t-1$  and  $t$  is shown in (35) considering the normal gas transmitting speed in gas pipelines. The constraints of the total volume of all the gas components are shown in (36) and (37). Based on Boyle's law [32], the relationship between the gas volume and pressure are shown in (38). The last constraint (39) ensures the balancing condition in the gas system.

$$0 \leq \{\}^{s,sub,t} \leq \{\}^{s,sub,max}, \{\} = P, Q \quad (16)$$

$$0 \leq r_{\{\},t}^+ \leq R_{\{\}}^+, \{\} = i_e, gt \quad (17)$$

$$0 \leq r_{\{\},t}^- \leq R_{\{\}}^-, \{\} = i_e, gt \quad (18)$$

$$P_{\{\},t}^s + r_{\{\},t}^+ \leq P_{\{\}}^{s,max}, \{\} = i_e, gt \quad (19)$$

$$P_{\{\},min} \leq P_{\{\},t}^s - r_{\{\},t}^-, \{\} = i_e, gt \quad (20)$$

$$0 \leq f_{\{\},t}^{s,s} \leq f_{\{\},max}^{s,s}, \{\} = a, r \quad (21)$$

$$\sum_{i_e \in I_e} P_{i_e,t}^s + \sum_{j \in J} \omega_{j,t}^{P,s} + \sum_{l_e \in L_e} f_{l_e,t}^{a,s,ini} - \sum_{l_e \in L_e} f_{l_e,t}^{a,s,ter} + \sum_{gt \in GT} P_{gt,t}^s \quad (22)$$

$$= \sum_{k_e \in K_e} P_{k_e,t} + \sum_{n \in N} P_{n,t}^{s,P2G}$$

$$\sum_{i_e \in I_e} Q_{i_e,t}^s + \sum_{j \in J} \omega_{j,t}^{Q,s} + \sum_{cb \in CB} Q_{cb,t}^s + \sum_{l_e \in L_e} f_{l_e,t}^{r,s,ini} - \sum_{l_e \in L_e} f_{l_e,t}^{r,s,ter} \quad (23)$$

$$= \sum_{k_e \in K_e} Q_{k_e,t}$$

$$G_{i_g,min} \leq G_{i_g,t}^s \leq G_{i_g,max} \quad (24)$$

$$Pr_{i_g,min}^2 \leq Pr_{i_g,t}^s \leq Pr_{i_g,max}^2 \quad (25)$$

$$Pr_{i_g,t}^{s,ini} \geq Pr_{i_g,t}^{s,ter} \quad (26)$$

$$f_{i_g,t}^{s,2} = \gamma_{i_g} (Pr_{i_g,t}^{s,ini} - Pr_{i_g,t}^{s,ter})^2 \quad (27)$$

$$0 \leq f_{i_g,t}^s \leq f_{i_g,max}^s \quad (28)$$

$$P_{gt,t}^s = c_{gt} f_{i_g,t}^s \quad (29)$$

$$\Omega_{n,t}^{mix} = \Omega_{hy}(\varphi_{n,t}^{hy,me} + \varphi_{n,t}^{hy,d}) + \Omega_{LPG} \varphi_{n,t}^{LPG} + \Omega_{ni} \varphi_{n,t}^{ni} + \Omega_{me} \varphi_{n,t}^{me} \quad (30)$$

$$SG_{n,t}^{mix} = [\rho_{hy}(\varphi_{n,t}^{hy,me} + \varphi_{n,t}^{hy,d}) + \rho_{LPG} \varphi_{n,t}^{LPG} + \rho_{ni} \varphi_{n,t}^{ni} + \rho_{me} \varphi_{n,t}^{me}] (\varphi_{n,t}^{hy,me} + \varphi_{n,t}^{hy,d} + \varphi_{n,t}^{LPG} + \varphi_{n,t}^{ni} + \varphi_{n,t}^{me}) \quad (31)$$

$$WI_{n,t}^{mix} = \Omega_{n,t}^{mix} / \sqrt{SG_{n,t}^{mix}} \quad (32)$$

$$CP_{n,t}^{mix} = O_i \frac{E_{hy}(\varphi_{n,t}^{hy,me} + \varphi_{n,t}^{hy,d}) + E_{LPG} \varphi_{n,t}^{LPG} + E_{ni} \varphi_{n,t}^{ni} + E_{me} \varphi_{n,t}^{me}}{\sqrt{SG_{n,t}^{mix}}} \quad (33)$$

$$\{\}^{min} \leq \{\} \leq \{\}^{max}, \quad (34)$$

$$\{\} = \Omega_{n,t}^{mix}, SG_{n,t}^{mix}, WI_{n,t}^{mix}, CP_{n,t}^{mix} \\ -\Delta \varphi_{n,max}^{s} \leq \varphi_{n,t}^{s} - \varphi_{n,t-1}^{s} \leq \Delta \varphi_{n,max}^{s} \quad (35)$$

$$\{\} = hy, me, hy, d, LPG, ni, me \\ \varphi_{n,t}^{hy,me} + \varphi_{n,t}^{hy,d} + \varphi_{n,t}^{LPG} + \varphi_{n,t}^{ni} + \varphi_{n,t}^{me} = \varphi_{n,t}^{mix} \quad (36)$$

$$\varphi_{n,min}^{mix} \leq \varphi_{n,t}^{mix} \leq \varphi_{n,max}^{mix} \quad (37)$$

$$\varphi_{n,t}^{mix} = \frac{\theta}{Pr_{n,t}} \quad (38)$$

$$\sum_{i_g \in I_g} G_{i_g,t}^s + \sum_{n \in N} G_{n,t}^{s,hy} + \sum_{l_g \in L_g} f_{l_g,t}^{s,ini} - \sum_{l_g \in L_g} f_{l_g,t}^{s,ter} \\ = \sum_{k_g \in K_g} G_{k_g,t} + \sum_{l_g \in L_g} f_{l_g,t}^{s,gt,t} \quad (39)$$

#### B. Real-Time Constraints of DR-VVPO

The real-time recourse VVPO can be implemented when the PV uncertainty is realized. The adjustment actions involve redispatching voltage regulating devices, traditional DGs and gas sources while providing the minimal load shedding schedule. In (40), the regulated output of generators is given. Constraint (41) limits both the power and gas load shedding. And the new balance constraints of power and gas systems are given in (42)-(44).

$$P_{\{\},t}^{re} - r_{\{\},t}^- \leq P_{\{\},t}^{re} \leq P_{\{\},t}^{re} + r_{\{\},t}^+, \{\} = i_e, gt \quad (40)$$

$$0 \leq P_{\{\},t}^{ls} \leq P_{\{\},max}^{ls}, \{\} = k_e, k_g \quad (41)$$

$$\sum_{i_e \in I_e} P_{i_e,t}^{re} + \sum_{j \in J} \xi_{j,t} + \sum_{gt \in GT} P_{gt,t}^s \quad (42)$$

$$+ \sum_{l_e \in L_e} f_{l_e,t}^{a,s,ini} - \sum_{l_e \in L_e} f_{l_e,t}^{a,s,ter}$$

$$= \sum_{k_e \in K_e} P_{k_e,t} - P_{k_e,t}^{ls} + \sum_{n \in N} P_{n,t}^{re,P2G}$$

$$\sum_{i_e \in I_e} Q_{i_e,t}^s + \sum_{j \in J} \omega_{j,t}^{Q,s} + \sum_{cb \in CB} Q_{cb,t}^s \quad (43)$$

$$+ \sum_{l_e \in L_e} f_{l_e,t}^{r,s,ini} - \sum_{l_e \in L_e} f_{l_e,t}^{r,s,ter}$$

$$= \sum_{k_e \in K_e} Q_{k_e,t} - Q_{k_e,t}^{ls}$$

TABLE I  
TWO-STAGE VVPO FRAMEWORK

|          | Decision variables                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | Objective                                                                                                                                                       | Uncertainty treatment                                       |
|----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------|
| Stage I  | $P_{sub,t}^s, Q_{sub,t}^s, P_{ie,t}^s, r_{ie,t}^+, r_{ie,t}^-, r_{gt,t}^+, r_{gt,t}^-, V_{b,t}^s, V_{sub,t}^s, TP_t^{s,OLTC}, \omega_{j,t}^{Q,s}, u_{cb,t}^s, Q_{cb,t}^s, f_{ie,t}^{a,s}, f_{ie,t}^{r,s}, Pr_{ig,t}^s, f_{ig,t}^s, G_{ig,t}^s, Pr_{ig,t}^s, \varphi_{n,t}^{s,hy,me}, \varphi_{n,t}^{s,LPG}, \varphi_{n,t}^{s,ni}, \varphi_{n,t}^{s,me}, \Omega_{n,t}^{s,mix}, SG_{n,t}^{s,mix}, WI_{n,t}^{s,mix}, CP_{n,t}^{s,mix}, \varphi_{n,t}^{s,mix}$                                            | Voltage deviation, Generation and reserve cost for traditional DGs and natural gas sources, power purchase cost from upper market and voltage deviation penalty | Renewable generation forecast                               |
| Stage II | $P_{sub,t}^{re}, Q_{sub,t}^{re}, P_{ie,t}^{re}, V_{b,t}^{re}, V_{sub,t}^{re}, TP_t^{re,OLTC}, \omega_{j,t}^{Q,re}, u_{cb,t}^{re}, Q_{cb,t}^{re}, f_{ie,t}^{a,re}, f_{ie,t}^{r,re}, Pr_{ig,t}^{re}, f_{ig,t}^{re}, G_{ig,t}^{re}, Pr_{ig,t}^{re}, \varphi_{n,t}^{s,hy,me}, \varphi_{n,t}^{s,hy,d}, \varphi_{n,t}^{s,LPG}, \varphi_{n,t}^{s,ni}, \varphi_{n,t}^{s,me}, \Omega_{n,t}^{s,mix}, SG_{n,t}^{s,mix}, WI_{n,t}^{s,mix}, CP_{n,t}^{s,mix}, \varphi_{n,t}^{s,mix}, P_{ke,t}^{ls}, P_{kg,t}^{ls}$ | Voltage deviation, Penalty cost for deviation of renewable, traditional DGs, natural gas sources, load shedding cost and voltage deviation penalty cost         | Uncertain renewable generation, based on moment information |

$$\sum_{i_g \in I_g} G_{i_g,t}^{re} + \sum_{i_g \in L_g} f_{i_g,t}^{re,ini} - \sum_{i_g \in L_g} f_{i_g,t}^{re,ter} \quad (44)$$

$$= \sum_{k_g \in K_g} G_{k_g,t} - G_{k_g,t}^{ls} + \sum_{i_g \in L_g} f_{i_g,t}^{re}$$

In addition to (40)-(44), the other constraints in the real-time stage are the same as the constraints of the first-stage when the superscript 's' is replaced by 're' due to the space limitation. Furthermore, the linearization is made for (16), (45) and (46), i.e.,  $|V_{b,t} - V_b^{ref}|, \{\cdot\} = s, re$  and  $|TP_t^{OLTC} - TP_{t-1}^{OLTC}|, \{\cdot\} = s, re$  are linearized via incorporating new auxiliary variables (refs). And McCormick inequality is used to relax constraints (17) and (19).

### C. Objective Function of DR-VVPO

The first-stage objective aims to minimize the total voltage deviation at all buses over all the time periods and the operation cost, which is given in (45). The first term transforms the voltage deviation to the monetary objective when it is multiplied by the penalty coefficient. Noted that other than the hydrogen injection to the gas pipelines, the additional mixture of LPG and nitrogen is required to ensure the satisfied gas quality indices, which are shown in the second and third terms. The power purchase from the day-ahead upper market is given as the fourth term. The rest of (45) presents the generation cost and reserve cost of traditional DGs and gas sources.

$$\Gamma_1 = \min \sum_{i_e \in I_e, i_g \in I_g, t \in T} \pi_v |V_{b,t}^s - V_b^{ref}| + \lambda_N^s \varphi_{n,t}^{s,ni} \quad (45)$$

$$+ \lambda_{LPG}^s \varphi_{n,t}^{s,LPG} + \lambda_{sub}^s P_{sub,t}^s + \lambda_{ie,t}^s P_{ie,t}^s + \lambda_{ie,t}^b P_{ie,t}^s + \lambda_{ie,t}^c + \lambda_{ig,t}^c P_{ig,t}^s + \lambda_{ie,t}^+ r_{ie,t}^+ + \lambda_{ie,t}^- r_{ie,t}^-$$

Equation (46) illustrates the second-stage objective including i) economic loss caused by voltage deviation, ii) regulation cost of implementing gas quality management, iii) real-time power purchase from the upper power market, iv) the cost of redispatching traditional DGs and gas sources and v) the cost of load shedding of power and gas systems.

$$\Gamma_2 = \min \sum_{i_e \in I_e, i_g \in I_g, t \in T, k_e \in K_e, k_g \in K_g} \pi_v |V_{b,t}^{re} - V_b^{ref}| \quad (46)$$

$$+ \lambda_N^{re} |\varphi_{n,t}^{re,ni} - \varphi_{n,t}^{s,ni}| + \lambda_{LPG}^{re} |\varphi_{n,t}^{re,LPG} - \varphi_{n,t}^{s,LPG}| + \lambda_{sub}^a P_{sub,t}^{re} + \lambda_j^{re} |\omega_{j,t}^s - \xi_{j,t}| + \lambda_{ie}^{re} |P_{ie,t}^s - P_{ie,t}^{re}| + \lambda_{ie}^{re} |P_{ig,t}^s - P_{ig,t}^{re}| + \lambda_{ke}^{ls} P_{ke,t}^{ls} + \lambda_{kg}^{ls} P_{kg,t}^{ls}$$

## IV. METHODOLOGY

In this section, the methodology for solving the DR-VVPO is given. To begin with, the original problem is presented via the abstract form of matrices and vectors. Then the ambiguity set construction for modelling the PV uncertainty is given. In the final step, dual reformulations are made. Noted that the DR-VVPO is a linear programming model. The integer variables, i.e.,  $TP_t^{re,OLTC}$  and  $u_{cb,t}^{re}$  are relaxed as continuous variables.

### A. Abstract Formulation

The compact form of the overall objective is given in (47) incorporating the first-stage and second-stage objective (45) and (46), which are represented by the first and second terms in (47), respectively. The constraints of the first and second stages are shown in (48) and (50).

$$\min_{x \in X} c'x + \sup_{P \in D} E_P[Q(x, \xi)] \quad (47)$$

$$\text{s.t. } Ax \leq b, \quad (48)$$

$$Q(x, \xi) = \min_y f'y \quad (49)$$

$$\text{s.t. } Ex + Fy + G\xi \leq h, \quad (50)$$

### B. Constructing the Ambiguity Set

Instead of optimizing under a deterministic set via RO, the ambiguity set of DRO enables to model the uncertainty with a set of possible distributions. This paper employs the moment-based ambiguity set. The fixed mean vector and covariance matrix are employed to support the moment information. Rather than modelling an explicit distribution via SO, DRO enables to model a variety of distributions based on fixed moment information. In (58), the ambiguity set is given, which only utilizes moment information to model all the possible uncertainty distributions, e.g., Gaussian distribution, Weibull distribution, etc [21, 33]. The expressions in the proposed ambiguity set represent the integral of the probability distribution of  $\xi$  is 1 and all the probability distributions are based on the same mean vector and covariance matrix.

$$D = \left\{ f(\xi) \left| \begin{array}{l} P\{\xi\} = 1 \\ E\{\xi\} = \mu \\ E\{\xi(\xi)'\} = \Sigma + \mu(\mu)' \end{array} \right. \right\} \quad (51)$$

### C. Second-stage Dual Formulation

In the second-stage objective, the 'sup min' framework needs to be reorganized as the dualized formulation with only 'min'. Hence a dual formulation is required. Accordingly, the objective functions of the first and second stages can be merged.

Write  $\sup_{Pf \in D} E_p[Q(x, \xi)]$  and (51) in its explicit form as (52)-(56) and  $Pf(\xi)$  represents the probability density function.

$$S(x)^{primal} = \max_{Pf \in D_\xi} \int_{\Xi} Q(x, \xi) Pf(\xi) d\xi \quad (52)$$

$$\text{s.t. } Pf(\xi) \geq 0, \forall \xi \in \Xi \quad (53)$$

$$\int_{\Xi} Pf(\xi) d\xi = 1 \quad (54)$$

$$\int_{\Xi} \xi^m Pf(\xi) d\xi = \mu_m, m=1,2, \dots, \Xi \quad (55)$$

$$\int_{\Xi} \xi^m \xi^n Pf(\xi) d\xi = \Sigma_{mn} + \mu_m \mu_n, m, n=1,2, \dots, \Xi \quad (56)$$

The decision variable of (52)-(56) is  $Pf(\xi)$  and there is an infinite number of variables given that the ambiguity set characterizes all the possible distributions. The dual reformulation is used to transform the infinite-dimensional primal form to a tractable dual form based on the strong duality theory [34]. The dual formulations are given in (57) and (58), which minimizes the dualized objective function based on the dual variables  $\psi_0$ ,  $\psi_j$  and  $\Psi_{jk}$ .

*Lemma:* the results of (57) are equal to those of (52) with the strictly positive covariance matrix and strong duality ensured [35].

Consequently, the primal form is successfully transferred to the dual form. The infinite number of variables are transformed into a finite number of variables. Noted that  $\theta$  represents  $\Sigma + \mu(\mu)'$  and the new compact form of DR-VVPO is given in (59).

$$S(x)^{dual} = \min_{\Psi, \psi, \psi_0} \langle \Psi' \theta \rangle + \psi' \mu + \psi_0 \quad (57)$$

$$\text{s.t. } (\xi)' \Psi \xi + \psi' \xi + \psi_0 \geq Q(x, \xi), \forall \xi \in \Xi \quad (58)$$

$$\min_{x \in X} c'x + S(x)^{dual} \quad (59)$$

#### D. Semidefinite Programming

After the dual reformulation, equation (59) contains a finite number of variables while an infinite number of constraints. Thus, it is required with a further transformation into a closed form of  $Q(x, \xi)$  to ensure computational tractability [36]. A new dual reformulation is made and given in (60) and (61) with the new dual variable  $\tau$ , where  $VS$  is the polyhedral set accommodating extreme points. And the positive quadratic function is obtained as the new representation of (49), where  $N_v$  is the vertex set of the feasible region in  $VS$ .

$$\max_{u \in VS} \tau'(h - Ex - G\xi) \quad (60)$$

$$VS = \{\tau | F'\tau = f, \tau \leq 0\} \quad (61)$$

Equation (62) represents that the optimal solution of (49) can be determined from extreme points in  $VS$ . Equations (63) and (64) can be further obtained when (58) is substituted by (62).

$$\exists \tau \in VS: Q(x, \xi) = (h - Ex - G\xi)' \tau \quad (62)$$

$$(\xi)' \Psi \xi + \psi' \xi + \psi_0 \geq (h - Ex - G\xi)' \tau \quad (63)$$

$$(\xi)' \Psi \xi + (\psi + G'\tau)' \xi + \psi_0 - (h - Ex)\tau^i \geq 0 \quad (64)$$

The positive quadratic function (64) can be given as the compact matrix form in (65), which is an SDP problem. Compared with (59), tractability is ensured within a closed form.

$$\min_{x, \Psi, \psi, \psi_0} c'x + \langle \Psi' \theta \rangle + \psi' \mu + \psi_0$$

$$\begin{bmatrix} \xi \\ 1 \end{bmatrix}' \begin{bmatrix} \Psi & \frac{1}{2}(\psi + G'\tau^i) \\ \frac{1}{2}(\psi + G'\tau^i)' & \psi_0 - (h - Ex)' \tau^i \end{bmatrix} \begin{bmatrix} \xi \\ 1 \end{bmatrix} \geq 0 \quad (65)$$

$$\forall \xi \in \Xi, i=1,2, \dots, N_v, x \in X, \forall \tau^i \in VS$$

#### V. CASE STUDIES

This section illustrates the effectiveness of the proposed DR-VVPO through 8 cases as shown in TABLE II. Cases 1 and 2 are used to compare the computational performance between RO and DRO. Cases 3-5 are used to show the impact of the gas system on voltage regulation. The impact of the capacity of regulating devices on voltage regulation is investigated among comparison between cases 2, 6 and 7. Case 8 is used to show the impact of gas quality management on DR-VVPO. A 33-bus20-node IES is shown in Fig. 2, with 3 traditional DGs, 4 PV systems and 7 capacitor banks connected [37]. The capacity for each capacitor bank and PV system are 400kVar and 360kVA, respectively. The interdependent power and gas systems are connected by three P2G facilities and two gas turbines. In TABLES III and IV, the parameters of natural gas sources and traditional DGs are given. The GCV and combustion potential index (CPI) for hydrogen, methane, LPG and nitrogen are given in TABLE V. The gas composition of original natural gas and LPG is provided in TABLE VI, mainly consisting of methane, ethane, propane and butane. LPG has high GCV but low CPI, which is used to increase WI and decrease CP. By contrast, the GCV and CPI of nitrogen are both zero, which enables a more flexible gas mixture.

##### A. Studies on Voltage Management

The voltage profiles for cases 2-5 are over all the periods are given in Fig. 3. The mean voltage profile over 24 hours is shown as the red dotted curve. For all the cases, the voltage magnitude drops from bus 1 to 18. Since the supply decreases at the same branch when it approaches the loads at the branch end. Then the voltage magnitude respectively from bus 18 to 20 and followed by the approximately decrease until bus 33. In case 2, besides the voltage at the main branch, i.e., buses 1-18, the voltage profile at buses 19, 23 and 26 are relatively higher than other buses. Cases 2 and 3 show similar voltage profile, i.e., ranging from 0.97 p.u. to 1.02 p.u.. The distinct difference can be found between bus 15-19. The voltage magnitude of case 3 is lower than those of case 2. The reason is that there is no gas-to-power (G2P) in case 3, which fails to supply extra support from the gas system. However, case 2 has two connections of G2P at buses 15 and 19. As for case 4, P2G facilities are not considered in the system topology. The obtained voltage profile is obviously different compared with cases 2 and 3. The voltage magnitude ranges between 0.97 p.u. and 1.03 p.u.. This case implies that P2G is effective for mitigating the voltage fluctuation via absorbing excessive PV generation. The distinct voltage profile differences are between buses 1-5 and buses 19-25. The power and gas systems are disconnected in case 5 and the voltage fluctuation is higher than that of cases 2 and 3, which ranges from 0.97 p.u. to 1.05 p.u..

The scheduling of OLTC tap positions for cases 2, 5-7 is given in Fig. 4. Case 5 results in the highest tap positions among the four considered cases. The reason is that without P2G connections, the fluctuation of PV systems causes higher power

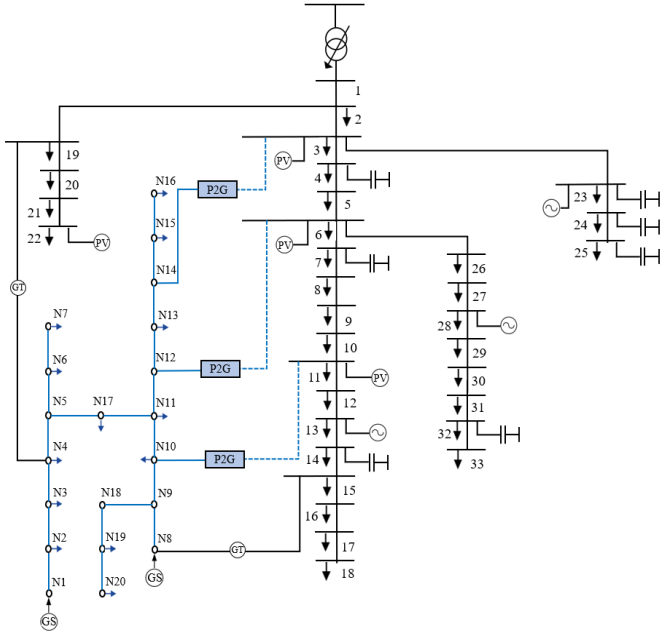


Fig. 2. The proposed 33-bus-20-node IES.

TABLE II  
CASE ILLUSTRATION

| Case No. | Optimization method | Capacitor bank capacity (kVar) | PV system capacity (kVA) | Gas system connection | Gas quality management |
|----------|---------------------|--------------------------------|--------------------------|-----------------------|------------------------|
| 1        | Robust              | 360                            | 400                      | Yes                   | Yes                    |
| 2        | DRO                 | 360                            | 400                      | Yes                   | Yes                    |
| 3        | DRO                 | 360                            | 400                      | P2G                   | Yes                    |
| 4        | DRO                 | 360                            | 400                      | G2P                   | Yes                    |
| 5        | DRO                 | 360                            | 400                      | No                    | Yes                    |
| 6        | DRO                 | 720                            | 400                      | Yes                   | Yes                    |
| 7        | DRO                 | 360                            | 800                      | Yes                   | Yes                    |
| 8        | DRO                 | 360                            | 400                      | Yes                   | No                     |

TABLE III  
PARAMETERS OF NATURAL GAS SOURCES

| Node No. | $P_{ig,min}$ (kcf/h) | $P_{ig,max}$ (kcf/h) | $\lambda_{ig}$ (\$/kcf) |
|----------|----------------------|----------------------|-------------------------|
| 1        | 1000                 | 6000                 | 2.2                     |
| 8        | 1000                 | 3000                 | 2                       |

TABLE IV  
GENERATOR PARAMETERS

| Bus No. | $P_{ig,max}$ (MW) | $P_{ig,min}$ (MW) | $R_{ig}^+, R_{ig}^-$ (MW) | $\lambda_{ig}^a$ (\$/MW) | $\lambda_{ig}^b$ (\$/MW) | $\lambda_{ig}^c$ (\$) |
|---------|-------------------|-------------------|---------------------------|--------------------------|--------------------------|-----------------------|
| 13      | 1.2               | 0.3               | 0.2                       | 6000                     | 7100                     | 6200                  |
| 23      | 1.2               | 0.3               | 0.2                       | 4500                     | 10500                    | 4000                  |
| 28      | 1.0               | 0.1               | 0.2                       | 4500                     | 10500                    | 4000                  |

TABLE V  
GCV AND CPI FOR DIFFERENT GASES

|     | H <sub>2</sub> | CH <sub>4</sub> | LPG | N <sub>2</sub> |
|-----|----------------|-----------------|-----|----------------|
| GCV | 10             | 40              | 115 | 0              |
| CPI | 100            | 50              | 42  | 0              |

TABLE VI  
GAS COMPOSITION (%)

|            | CH <sub>4</sub> | C <sub>2</sub> H <sub>6</sub> | C <sub>3</sub> H <sub>8</sub> | C <sub>4</sub> H <sub>10</sub> | CO <sub>2</sub> | Other |
|------------|-----------------|-------------------------------|-------------------------------|--------------------------------|-----------------|-------|
| Natura gas | 79.6            | 8.3                           | 4.9                           | 1.4                            | 3.4             | 2.4   |
| LPG        | 91.1            | 4.3                           | 3.0                           | 1.4                            | 0               | 0.2   |

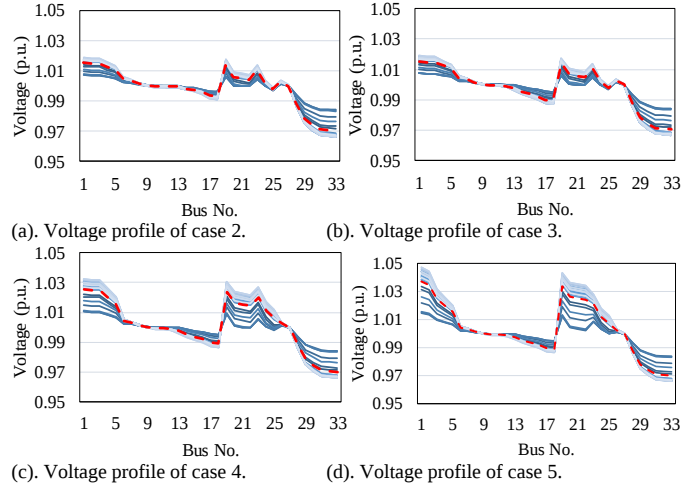


Fig. 3. Expected real-time voltage profiles for cases 2, 3, 4 and 5.

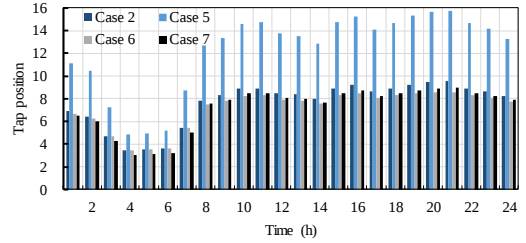


Fig. 4. OLTC tap position for cases 2, 5, 6 and 7.

flow and thus affect the high voltage issues. The tap position decreases from +11 to +5 between 1:00 and 4:00. It rises after 7:00, followed by a fluctuation afterwards. It peaks at +16 at 20:00 during the peak-load time period, which also witnesses the highest tap position of other cases. Cases 2, 6 and 7 show similar tap profile, which indicates that the additional capacity of capacitor banks and PV systems result in lower impact compared with employing P2G facilities.

### B. Studies on Economic Performance

In TABLE VII, the operation cost for both the first and second stages are shown. Case 5 yields the highest operation cost at the two stages, i.e., \$502542 and \$127567. The reason is that case 5 is studied in a pure power system without any cost-effective supply from gas sources. In comparison, the total operation cost of case 8 is the lowest, \$474967, which is only 75% of case 5. The reason is that gas quality management is not conducted which avoids the high purchase cost of LPG and nitrogen to maintain the permitted gas quality. Cases 1 and 2 deal with the PV uncertainty via RO and DRO, respectively. The single-stage RO provides a higher total operation cost (\$548440) than that of DRO (\$546692). And even the single-stage operation cost is higher than the sum of the cost of first and second stages via DRO. This proves the over-conservatism of RO as it considers the worst-case of PV output. The two-stage DRO mitigates the conservatism by providing a 'here-and-now' and 'wait-and-see' hierarchical framework with flexibility on dispatch adjustment and incorporates the distribution information in the ambiguity set. Cases 3 and 4 consider a single connection between power and gas systems. The results show that case 4 yields a higher cost than that of

TABLE VII  
ECONOMIC PERFORMANCE FOR CASES 1-8

| Economic result                 | Case 1 | Case 2 | Case 3 | Case 4 |
|---------------------------------|--------|--------|--------|--------|
| First-stage cost (\$)           | 548440 | 481711 | 495904 | 497171 |
| Expected Second-stage cost (\$) | 0      | 64981  | 65325  | 122795 |
| Total cost (\$)                 | 548440 | 546692 | 561229 | 619967 |
| Economic result                 | Case 5 | Case 6 | Case 7 | Case 8 |
| First-stage cost (\$)           | 502542 | 478013 | 476511 | 421013 |
| Expected Second-stage cost (\$) | 127567 | 64390  | 63886  | 53954  |
| Total cost (\$)                 | 630109 | 542403 | 540396 | 474967 |

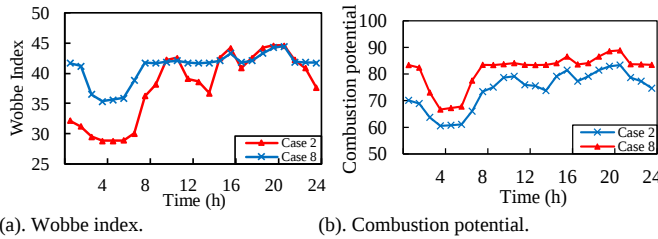


Fig. 5. Gas quality indices for cases 2 and 8.

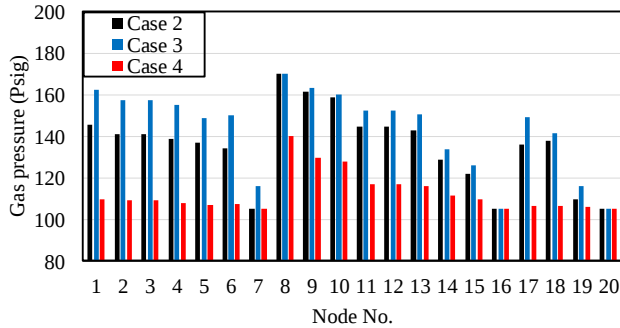


Fig. 6. Gas pressure for cases 2, 3 and 4.

case 3, which implies that the three P2G facilities are essential for improving the economic efficiency by transforming the surplus PV generation to gas loads. Compared with case 2, cases 3 and 4 have lower operation cost, which indicates the advantages of coordination and complementation of IES on system economic efficiency compared with the single operating power system. Cases 6 and 7 result in lower operating cost compared with case 2 due to their larger capacity of PV systems and capacitor banks.

### C. Studies on Gas Quality Management

The gas quality management strategy of VVPO is proposed in this subsection, considering four quality indices and the gas pressure variation at each node. Fig. 5 depicts the variation of gas quality indices at node 10. The comparison is made between the benchmark case 2 and case 8 without gas quality management considered. Overall, case 2 shows higher WI compared with case 8. But the CP of case 2 shows lower results than case 8. It is to be noted that the permitted WI range is between 35 and 50. However, case 8 results in WI that is lower than the lower limit before 8:00. The low WI will lead to ignition problems, i.e., more gas amount is required for ignition

TABLE VIII  
CASE ILLUSTRATION

| Case No. | Capacitor bank capacity (kVA) | PV system capacity (kVA) | Gas system connection |
|----------|-------------------------------|--------------------------|-----------------------|
| 1        | 360                           | 800                      | Two                   |
| 2        | 720                           | 800                      | Two                   |
| 3        | 360                           | 1600                     | Two                   |
| 4        | 360                           | 800                      | No                    |

TABLE IX  
COST OF EACH STAGE

| Economic result                 | Case 1 | Case 2 | Case 3 | Case 4 |
|---------------------------------|--------|--------|--------|--------|
| First-stage cost (\$)           | 47274  | 46052  | 42723  | 51868  |
| Expected Second-stage cost (\$) | 3190   | 3074   | 3055   | 4012   |
| Total cost (\$)                 | 50464  | 49126  | 45778  | 55880  |

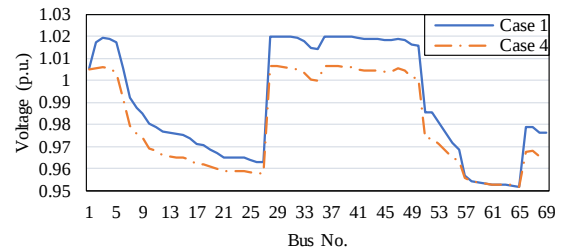


Fig. 7. Expected real-time voltage profiles for cases 1 and 4.

on the same gas equipment. Meanwhile, an unstable flame will be possibly caused. The CP is given in Fig. 5 (b), which shows that the CP if case 8 is higher than case 2 which shows that the hydrogen amount of case 8 is more than that of case 2. However, this is dangerous as inefficient combustion and even gas explosion might occur. In Fig. 6, the gas pressure is scheduled based on the optimal gas quality management. Cases 2-4 are studied with different system interconnections. The pressures at nodes 1 and 8 are higher than that of other nodes because of the direct connection of natural gas sources. The pressure decreases along the direction of gas flow. Nevertheless, another pressure peak occurs at gas node 17 when the gas flow from the two branches gather and supply node 17. Case 3 presents the highest pressure at all nodes compared with cases 2 and 4. Since the single connection from power to the gas system provides additional supply via P2G facilities.

### D. Scalability Analysis

The scalability study is conducted in a 69-bus-20-node IES. There are 6 PV systems connected at buses 9, 23, 26, 34, 44 and 58, respectively. The 12 capacitor banks and transformer are used to compensate the reactive power. The 20-node gas system contains two natural gas sources and two gas turbines, which are connected between the gas and power systems. The data can be found in [37]. This section considers 4 cases which are shown in TABLE VIII.

As given in TABLE IX, case 4 has the highest total cost while case 3 has the lowest total cost. Compared with the benchmark case, i.e., case 1, there is no connection between electricity and gas systems in case 4. The capacity of capacitor banks and PV

systems are twice as case 1 in cases 2 and 3, yielding \$1338 and \$4686 less operation cost.

In Fig. 7, the voltage profiles of cases 1 and 2 are studied to investigate the impact from gas system connection. In case 1, it can be seen that the voltage level is decreasing along the main branch from bus 5 to bus 28. And the voltage level remains approximately the same value between bus 28 and bus 50 at 1.02 p.u.. With two gas turbines connected, the voltage level ranges from 0.952 p.u. to 1.020 p.u.. With only one connection with the gas system, the voltage level is lower than that of case 1, which ranges from 0.952 p.u. to 1.007 p.u.. Compared with case 1, when no gas turbines equipped, the voltage profile decreases by 0.8% in case 2. The comparison between cases 1 and 2 shows the increase of the voltage level for all buses with the addition of gas system connection.

### E. Discussion on the Results

This section summarizes the results obtained from the extensive case studies in section V. The economic studies on 8 cases in 33-bus-20-node and 69-bus-20-node IESs indicate that i) DRO is effective on mitigating the conservatism of RO; ii) The doubled PV capacity is effective for reducing the overall operation cost. iii) Omitting the gas quality management will effectively decrease the operation cost.

The voltage profile results show that the gas system enables to address the voltage fluctuation through offsetting the surplus power generation. Moreover, the traditional voltage regulating devices, i.e., PV systems, OLTC and capacitor banks also provide effective voltage regulation measures. However, the proposed gas quality management has a minor impact on VVO. The results of the gas quality indices and gas pressure study show that without the gas quality management, the proposed 4 gas quality indices are violated. Accordingly, the joint optimization of VVO and gas pressure is highly essential for ensuring both voltage profiles and high-quality gas supply.

The total computation time is approximately two hours, where the first-stage problem takes most of the time since the vertex set is extremely vast and the approach to find the optimality is time-consuming. However, when  $O^*$  and  $x^*$  are obtained, the real-time stage only takes averagely 30 seconds with 1000 simulation samples. Thus, the computational time of the real-time stage is acceptable in practice.

In addition to the proposed VVPO model, Volt-VAR-droop control (VVDC) has been designed for local voltage regulations to obtain stable frequency. Existing papers have extensively investigated VVDC models considering uncertainties based on data-driven scenario approaches or robust control [14,15]. However, VVDC is not viable to be resolved by DRO at present, as DRO requires fully linearized and static mathematical formulations. Currently, stochastic or robust approaches are more practical to solve VVDC. And the distributionally robust control model is out of the scope of this paper.

There are many remaining challenges in the current VVPO model and four major ones are as follows:

- Various energy storage systems in IES, including battery, gas and hydrogen, which be incorporated into the VVPO model for helping voltage regulations.
- It will investigate the volt-VAR control and the feasibility of combining it with the proposed two-stage DRO approach.

- Gas quality management may cause congestion issues for gas pipelines due to the admixture of hydrogen, nitrogen and LPG. Therefore, gas pipeline congestion will be considered and managed.
- Uncertain PV fluctuations could occur at the minute level. Therefore, a multi-timescale VVPO model containing finer temporal resolution will be investigated, particularly combined with the DRO approach.

## VI. CONCLUSION

A two-stage VVPO model is developed to regulate voltage deviation, manage gas quality and minimize system operation cost of IES. Emerging P2G facilities are applied for voltage regulation via transferring excessive PV energy to hydrogen and transported in the gas system. The novel gas quality management is proposed for satisfying gas quality standards. The two-stage DRO is utilized to capture PV uncertainty and the reformulated SDP problem is solved efficiently by CGA. Some key findings are given:

- P2G facilities effectively contribute to voltage management.
- A secure IES operation is realized based on the proposed gas quality management strategy.
- Compared to the pure power system, the system operation cost in IES with interconnections is reduced greatly.
- The optimal coordination of energy conversion technologies enables to improve the energy utilization efficiency.

The proposed DR-VVPO presents a practical operation scheme for system operators for ensuring the voltage profile security and gas quality with lower operation cost under the multi-energy and high renewable integration era.

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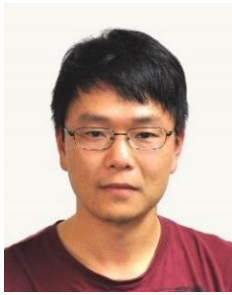


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