

## Membrane Separations

### Problem set #3 (deadline 10-1-03)

1. A commercial polyvinyl alcohol (PVA) pervaporation membrane will be utilised to partially dehydrate an ethanol(1)/water(2) mixture containing 75.8% ethanol at a feed temperature of 60°C. Since PVA membranes are hydrophilic, water will selectively permeate across the membrane. The resulting permeate was found to contain 9.0 wt% ethanol. Given that the permeate flux is 0.40 kg/m<sup>2</sup>·h, calculate values of permeability coefficient for water and ethanol if the outlet pressure is 76 mmHg. Recall that the driving force in pervaporation is a difference of chemical potential (or fugacity, or activity), and that the molar flux is equal to the permeability times the driving force. Assume ideal gas and non-ideal liquid behaviour when calculating fugacities.

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2. A liquid containing dilute solute A at a concentration  $c_1=0.030 \text{ kmol/m}^3$  is flowing rapidly by a membrane of thickness  $L=3.0 \cdot 10^{-5} \text{ m}$ . The distribution coefficient  $K'=1.5$  and  $D_{AB}=7.0 \cdot 10^{-11} \text{ m}^2/\text{s}$  in the membrane. The solute diffuses through the membrane and its concentration on the other side is  $c_2=0.0050 \text{ kmol/m}^3$ . The mass transfer coefficient  $k_{c1}$  is large and can be considered as infinite and  $k_{c2}=2.02 \cdot 10^{-5} \text{ m/s}$ .

a) Derive the equation to calculate the steady-state flux  $N_A$  and make a sketch.

b) Calculate the flux and the concentrations at the membrane interfaces.

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3. Experiments at 25 °C were performed to determine the permeabilities of a cellulose acetate membrane. The laboratory test section has a membrane area  $A=2 \cdot 10^{-3} \text{ m}^2$ . The inlet feed solution concentration of NaCl is  $c_1=10 \text{ g NaCl/L solution}$  ( $\rho_1=1004 \text{ kg sol./m}^3$ ). The water recovery is assumed low so that the concentration  $c_1$  in the entering feed solution flowing past the membrane and the concentration of the reject solution are equal. The product solution contains  $c_2=0.39 \text{ g NaCl/L sol.}$  ( $\rho_2=997 \text{ kg sol./m}^3$ ) and its flow rate is  $1.92 \cdot 10^{-8} \text{ m}^3 \text{ sol./s}$ . A pressure differential of 5514 kPa (54.42 atm) is used. Calculate the permeability constants and the solute rejection  $R$ .